

NTSE STAGE – I (DELHI STATE)
05 – A (2019 – 20)
(For Class – X)
MENTAL ABILITY TEST (MAT)

ANSWER KEYS

1.	2 2 or	2.	4	3.	1	4.	8. 1
5.	4 3 4	6.	4	7.	1	12.	2
9.	3 3 4	10.	2	11.	2	16.	2
13.	3 2 4 1	14.	2	15.	4	20.	4
17.	1 4 4	18.	2	19.	4	24.	3
21.	2 2 1 1	22.	2	23.	3	28.	2
25.	3 3 2	26.	2	27.	2	32.	3
29.		30.	*	31.	1	36.	3
33.		34.	4	35.	1	40.	*
37.		38.	2	39.	3	44.	1
41.		42.	4	43.	4	48.	1
45.		46.	1	47.	2	52.	3
49.		50.	3	51.	1	56.	3
53.		54.	1	55.	1	60.	3
57.		58.	2	59.	2	64.	3.
61.		62.	2	63.	1	68.	4
65.		66.	3	67.	1	72.	2
69.		70.	4	71.	2	76.	4
73.		74.	1	75.	2	80.	3
77.		78.	4	79.	2	84.	3
81.		82.	2	83.	3	88.	4
85.	1	86.	*	87.	3	92.	2
89.	1	90.	3	91.	3	96.	3
93.	1	94.	*	95.	3	100.	4
97.	4	98.	3	99.	1		2

Observations:

30. In question it is mentioned as LCF & also the algebraic expressions are not given in English part. So, this makes the question incomplete, but according to Hindi part the best possible answer is 1. Incomplete question in English part but according to Hindi part it should be 3
36. No option correct No option correct
- 86.
- 94.

NTSE STAGE – I (DELHI STATE)
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 MENTAL ABILITY TEST (MAT)
 HINTS & SOLUTIONS

1. 2
 1. Positive factors of 256 are
 1, 2, 4, 8, 16, 32, 64, 128, 256

$$S_q = \frac{a(r^n - 1)}{r - 1}$$
 [where a = 1, and r = 2, and n = 9]

$$S_9 = 511$$

2. 4

$$\frac{x}{x-1} - \frac{x-1}{x} = \frac{1}{x(x-1)} - \frac{x^2 - 1}{x(x-1)}$$

$$= \frac{x^2 - (x^2 - 1)}{x(x-1)} = \frac{1}{x(x-1)}$$

$$= 2$$

3. 1
 3. 5 + 6 + 7 + ... + 19
 Here a = 5, d = 1 and n = 15

$$S_n = \frac{n}{2} [2a + (n-1)d]$$

$$S_{15} = \frac{15}{2} [10 + 14] = \frac{15}{2} \times 24$$

$$= 15 \times 12 = 180$$

4. 1
 4. $1 : 2 : 3 :: 6 : 8 : 9$
 $\frac{1}{2} : \frac{2}{3} : \frac{3}{4}$
 Let numbers be 6x, 8x and 9x
 $9x - 6x = 27$
 $x = 9$
 Numbers are 54, 72, 81

5. 2 or 4
 5. $3^{25} + 3^{26} + 3^{27} + 3^{28} + 3^{25} + 3^0 + 3^1 + 3^2 + 3^3$
 $= 3 \cdot 25 + 1 + 3 + 9 + 27$
 $= 325 + 40 + 323 + 9 + 58$
 $= 325 + 40 + 323 + 845$

6. 4
 6. Rohan's final score = $\frac{90 + 2 + 75 + 1}{3}$
 $= 85$

7. 1 Let Grand mother = G, mother = M and daughter = D
 7. D Possible ways = GMD
 GDM
 MGD MDG DGM
 DMG

8. 2
 8. Let at time of marriage man's age = x years
 And man's wife's age = y years
 $x = y + 6 \dots(1)$
 And $x = \frac{2}{5}y + 12$
 $= 5x + 60 = 6y + 72$
 $= 5x - 6y = 12 \dots(2)$
 Solving both equations we got x = 24 and y = 18

9. 3
 9. P (number is even) = $\frac{1}{2}$

P (number is less than 4) = $\frac{1}{2}$

P (number is even and less than 4) = $\frac{1}{6}$

$P(\text{number is less than 4} \cap \text{number is even}) = \frac{1}{6}$
 $P(\text{number is even}) = \frac{1}{2}$
 $P(\text{number is even and less than 4}) = \frac{1}{6}$

10. 2
 10. 10 balls 5B and 5W
 After removing 1 B balls, total balls left = 9 and
 Total black balls left = 4
 $P(\text{B ball after removing 1st B ball}) = \frac{4}{9}$

11. 2
 11. $10 - 3 = 12 \cap 10 - 3 + 5 = 12$
 $12 - 4 = 13 \cap 12 - 4 + 5 = 13$
 $13 - 5 = 14 \cap 13 - 5 + 5 = 14$
 $14 - 6 = ? \cap 14 - 6 + 5 = 15$

12. 2
 12. If bus does not stops, then it will travel 9 km more with 54 kmph
 $\text{It will stop for } \frac{9}{54} \text{ hr} = \frac{9}{54} \times 60 \text{ min} = 10 \text{ min}$

13. 4

13.
$$\frac{40 \times 1620 + 30 \times 960 + x \times 5200}{100 + 100 + 100} = 40 \times 1620 + 30 \times 960 + 5200$$

$x = 18$

14. 2
 14. Between 1st and 25th tree there are 24 gaps & let say each gap is of x m distance.
 $24x = 30$

$x = \frac{3}{4}$

Now between 3rd & 15th tree there are 12 gaps
 $\text{Distance between 3rd \& 15th tree} = 12 \times \frac{3}{4} = 9 \text{ m}$

15. 4

15.	Time	8	8:30	9	9:30	10	10:30	11	11:30	12	12:30	1	1:30
	Bell	3	1	1	1	3	3	1	1	1	1	1	3

\square Bell rung 20 times.

16. 4

16. $\frac{80A + 50B}{100 + 100}$

or $\frac{B}{A} = \frac{8}{5}$

Now $B = \frac{x}{100} A$ & $\frac{B}{A} = 100$

$x = \frac{8}{5} \times 100 = 160$

17. 3
 17. Let numbers = $(x - 2), (x - 1), (x + 1), (x + 2)$

$$\frac{x^2 - 2^2 + x^2 - 1^2 + x^2 + 1^2 + x^2 + 2^2}{4} = 7$$

$5x = 7$

$x = 7$

highest number = 9

18. 2

18. $x^3 + y^3 + z^3 + 3xyz = (x + y + z)(x^2 + y^2 + z^2 + xy + yz + zx)$

Now we know that, $x^2 + y^2 + z^2 + 2xy + yz + zx = 15^2 + 15^2 + 51^2 + 87$

$xy + yz + zx = \frac{15^2 + 15^2 + 51^2 + 87}{2} = 87$

$x^3 + y^3 + z^3 + 3xyz = 15^3 + 15^3 + 51^3 + 87 = 15 \times (36) = 540$

19. 4
 19. Let sides = 3x, 4x & 5x cm

$$S = \frac{3x + 4x + 5x}{2} + 6x$$

$$\text{Area} = \sqrt{S(S-a)(S-b)(S-c)}$$

$$384 = \sqrt{3x(2x+x)}$$

$$384 = 6x^2$$

$$x = 8$$

$$P = 12x = 12 \times 8 = 96 \text{ cm}$$

20. 3

20. (1) $\frac{1}{3 \times \frac{1}{17}} + \frac{1}{3 \times \frac{16}{17}} + \frac{17}{66}$

(2) $\frac{1}{3 \times \frac{1}{1 \times \frac{1}{9}}} + \frac{1}{3 \times \frac{1}{17}} + \frac{1}{60} + \frac{17}{60}$

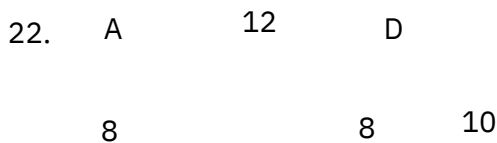
(3) $\frac{1}{3 \times \frac{1}{1 \times \frac{1}{4}}} + \frac{1}{3 \times \frac{1}{13}} + \frac{1}{48} + \frac{13}{48}$

(4) $\frac{1}{3 \times \frac{1}{9}} + \frac{1}{\frac{35}{8}} + \frac{8}{35}$

21. 3

21. $a \$ b = a \times (a + b)$
 $(2 \$ 0) \$ 1 = [2 \times (2 + 0)] \$ 1$
 $= 4 \$ 1$
 $= 4 \times (4 + 1)$
 $= 20$

22. 2



B E 6 C

Construction: Draw $DE \parallel BC$

□ Area of ABCD = Area of rec ABED + Area of $\square DEC$

$$= 8 \times 12 + \frac{1}{2} \times 6 \times 8$$

$$= 96 + 24 = 120 \text{ m}^2$$

23. 3

23. 4, 8, 28, 80, 244

$\underbrace{\quad\quad\quad}_{\times 3 - 4}$
 $\underbrace{\quad\quad\quad}_{\times 3 + 4}$
 $\underbrace{\quad\quad\quad}_{\times 3 - 4}$
 $\underbrace{\quad\quad\quad}_{\times 3 + 4}$

24. 2
24. 4, 7, 12, 19, 28, 39, 52

$\underbrace{\quad\quad\quad}_{+3}$
 $\underbrace{\quad\quad\quad}_{+5}$
 $\underbrace{\quad\quad\quad}_{+7}$
 $\underbrace{\quad\quad\quad}_{+9}$
 $\underbrace{\quad\quad\quad}_{+11}$
 $\underbrace{\quad\quad\quad}_{+13}$

25. 4
25. 10080, 1680, 336, 84, 28, 14

\square_6
 \square_5
 \square_4
 \square_3
 \square_2

26. 2
26. CI $\square \square \square \square$ P $\square \square \square \square$ 1 $\square \square \square \square$ 100 $\square \square \square \square$ 1 $\square \square \square \square$

$\square \square \square \square$ 4347 $\square \square \square \square$ 300 00 $\square \square \square \square$ 1 $\square \square \square \square$ 7 $\square \square \square \square$ 100 $\square \square \square \square$ 1 $\square \square \square \square$

$\square \square \square \square$ $\frac{1149}{0}$ $\square \square \square \square$ $\frac{107}{100}$ $\square \square \square \square$

$\square \square \square \square$ $\frac{1000}{107}$ $\square \square \square \square$ $\frac{107}{100}$ $\square \square \square \square$

$\square n = 2$

27. 2
27. $2^{\frac{1}{2}}, 9^{\frac{1}{3}}, 16^{\frac{1}{4}}, 32^{\frac{1}{5}}$

$= 2^{\frac{1}{2}}, 9^{\frac{1}{3}}, 21, 21$

$\square \square \square \square$ $2^{\frac{6}{6}}, 9^{\frac{6}{6}}, 26, 26$

$= 23, 92, 26, 26$

28. 3
28. $x \square \frac{1}{19} \square 2$

$\square x$
 $\square x^2 + 1 - 2x = 0$
 $\square (x - 1)^2 = 0$
 $\square x = 1$

$x \square 17 \square \frac{1}{19} \square 117 \square \frac{1}{119} \square 2$

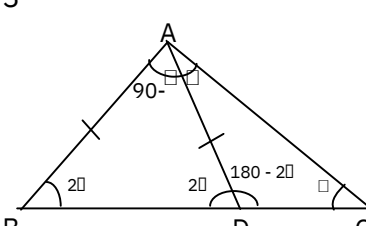
29. 3
29. Let runs required = x

$\square 15 \square 6 + x \square 5 = 7.2 \square 20$
 $\square x = 54$

$\square \text{required run rate} = \frac{54}{5} \square 10.8$

30. 1
 30. $P + Q = x + y, PQ = xy$
 $(P + Q)^3 = P^3 + Q^3 + 3PQ(P + Q)$
 $\therefore P^3 + Q^3 = (x + y)^3 - 3xy(x + y) = x^3 + y^3$

31. 1
 31. $\frac{x \times 5}{12} = \frac{x}{16} \times 1$
 $\frac{4x}{203x} = 1$
 $x = \frac{48 \times 20}{7} = \frac{28}{7} = 4$
 $x = 4 \text{ min}$

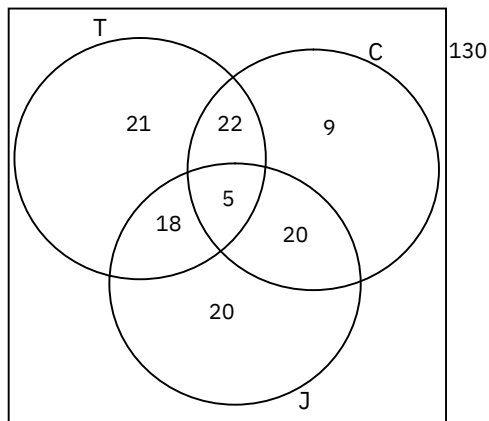
32. 3
 32. 
 In $\triangle ABD, 90 - x + 2x + 2x = 180^\circ$
 $4x - x = 90 \dots (1)$
 In $\triangle ABC, 3x + 90 = 180^\circ$
 $3x = 90 \dots (2)$
 $x = 30^\circ$
 $2x = 60^\circ$
 $180 - 2x = 120^\circ$

33. 2
 33. Since shaded region has $\frac{1}{6}$ of area of circle
 $\therefore \theta$ in shaded region = $\frac{360}{6} = 60^\circ$
 $\therefore \theta$ in Arc AQB = $360 - 120 = 240$
 \therefore length of arc AQB = $\frac{240}{360} \times 2\pi r$
 $= \frac{2}{3} \times 2 \times \pi \times 10$
 $= \frac{40\pi}{3}$

34. 4
 34. Let original length = a cm & width = b cm
 \therefore Original Area = $ab \text{ cm}^2$
 New area = $\frac{12}{5} \times \frac{80}{100} ab = \frac{8}{5} ab \text{ cm}^2$
 Since original area = new area
 \therefore no change in area

35. 1

35.



36. 3 (Incomplete question in English language but according to hindi part it should be 3 (35))

36.

Let 3 nos = x, y & z

$$\square x + y = 55 \text{ ---- (1)}$$

$$y + z = 65 \text{ ---- (2)}$$

$$3x + z = 110 \text{ ---- (3)}$$

Form eq (1) & (2)

$$55 - x + z = 65$$

$$\square z - x = 10 \text{ ---- (4)}$$

From eq (3) & (4)

$$3x + z + 3z - 3x = 110 + 30$$

$$z \square \frac{140}{4} \square 35$$

37. 4

37. For K ratio = $\frac{6000}{12000} \square \frac{1}{2}$

For L ratio = $\frac{5400}{6000} \square \frac{9}{10}$

For M ratio = $\frac{12000}{21000} \square \frac{4}{7}$

For N ratio = $\frac{4200}{9000} \square \frac{7}{15}$

For O ratio = $\frac{7500}{12000} \square \frac{5}{8}$

Clearly N has the minimum ratio

38. 2

38. For K ratio = $\frac{2400}{27000} \square 0.088$

For L ratio = $\frac{1200}{15000} \square 0.08$

For M ratio = $\frac{4500}{45000} \square 0.10$

For N ratio = $\frac{2400}{21000} \square 0.114$

For O ratio = $\frac{3000}{30000} \square 0.10$

Clearly N has maximum bonus in comparison to his total income.

39. 3

39. For K = $\frac{12000}{27000} \times 100 = 44.44\%$
 For L = $\frac{6000}{15000} \times 100 = 40\%$
 For M = $\frac{21000}{45000} \times 100 = 46.66\%$
 For N = $\frac{9000}{21000} \times 100 = 42.85\%$
 For O = $\frac{12000}{30000} \times 100 = 40\%$

Clearly M has maximum percentage

40. 1

40. $\frac{6000}{7500} \times 100 = 80\%$

41. 1

41. $\frac{M}{S} = \frac{4}{5}$
 $M = 4n, S = 5n$
 $\frac{M}{S} = \frac{57}{59}$
 $\frac{4n}{5n} = \frac{7}{9}$
 $36n - 45 = 35n - 35$
 $n = 10$
 Present ages are 40 and 50 years.

42. 4

42. Number of different combinations = ${}^3C_1 \times {}^4C_1 \times {}^2C_1$
 $= \frac{3!}{1! \times 2!} \times \frac{4!}{1! \times 3!} \times \frac{2!}{1! \times 1!} = 4 = 24$

43. 4

43. Let original length = l
 And original breadth = b
 \square Original area = lb
 New area = $\frac{112.5}{100} \times \frac{90b}{100}$
 $= 1.0125 lb$
 \square Charge in area = $\frac{(1.0125 - 1)}{1} \times 100 = 1.25\%$ increase

44. 1

44. $x =$ Even number
 $P =$ Odd number
 (1) Odd - Even - 1 = Even \square Odd
 (2) Odd + Even + 1 = Even = Even
 (3) Odd \times Even + Odd = Odd = Odd
 (4) Odd² + Even² + 1 = Even = Even

45. 1

45. Volume of liquid in cuboidal container
= Volume of liquid in cylindrical container

$$l \times b \times h = \pi r^2 h$$

$$2 \times 10 \times 20 = \pi \times 52 \times h$$

$$h = \frac{400}{25} = 16$$

46. 1
46. $\tan \theta + \cot \theta = 2$

$$\tan \theta = \frac{1}{\tan \theta} \Rightarrow \tan^2 \theta = 1; \quad \frac{\tan^2 \theta - 1}{\tan \theta} = 2$$

$$\tan^2 \theta - 2 \tan \theta + 1 = 0$$

$$(\tan \theta - 1)^2 = 0$$

$$\tan \theta = 1$$

$$\cot \theta = 1$$

$$\tan \theta + \cot \theta = 1 + 1$$

$$1 + 1 = 2$$

47. 2

47. $2(a + b)^4 = (a^2 + b^2 + 2ab)^2$
 $= (a^2 + b^2 + 2ab)^2$
 $= a^4 + b^4 + 4a^2b^2 + 4a^3b + 2a^2b^2 + 4ab^3$
 $= a^4 + b^4 + 6a^2b^2 + 4a^3b + 4ab^3$

$$\text{Coefficient of } a^2b^2 = 6.$$

48. 3

48. $\frac{\text{Girls}}{\text{Total class}} = \frac{x}{y}$

49. 4

49. $26n - 42n$

$$64n - 16n$$

We know that $a^n - b^n$ is always divisible by $(a - b)$

$$\Rightarrow 64n - 16n \text{ is divisible by } 48.$$

50. 3

50. $x - 2 = \frac{22}{3} - \frac{21}{3}$

$$x - 2 = \frac{22}{3} - \frac{21}{3}$$

Cubing both sides

$$x^3 - 8 - 3(2x)(x - 2) = \frac{22}{3} - \frac{21}{3} - 3\left(\frac{22}{3} - \frac{21}{3}\right)(x - 2)$$

$$\Rightarrow x^3 - 8 - 6x^2 + 12x = 4 - 2 - 6x + 12$$

$$\Rightarrow x^3 - 6x^2 + 18x = 22$$

$$\Rightarrow x^3 - 6x^2 + 18x + 18 = 40$$

51. 1 1 figure $\Rightarrow s = 6$ 2

51. figure $\Rightarrow s = 4$ 3

- figure $\Rightarrow s = 2$ 1

Total number of

$$\Rightarrow s = 12$$

52. 3

52. F ather (Ketan's

|

Ketan (Amit's father)

|

Amit

53. 4

53. si po re □ book is thick ... (1)

ti na re □ bag is heavy ... (2)

ka si □ interesting book ... (3)

de ti □ that bag ... (4)

From (2) & (4) code of 'bag' = ti, so code of 'that' = de

From (1) & (2) code of 'is' is re

From (1) & (3) code of 'book' = si, so code of 'interesting' = ka

□ code of that bag is interesting' = de ti re ka

54. 1

54. P R I N C I P A L
| | | | | | | | |

M B O Q S O M V W

T E A C H E R

| | | | |

F D V S Z D B

C A P I T A L

So,

S V M O F V W

55. 1

55. R O P E D O U B T L I V E

| , ,

% 5 7 \$ 3 5 # 8 * @ 2 4 \$

□ T R O U B L E
| | | | | | | |

* % 5 # 8 @ \$

56. 3

56. \$ □ □ □ +

□ □ □ -

@ □ □ □ □

*□□□□

$$\begin{aligned}
16 \$ 4 @ 5 \# 72 * 8 &= 16 + 4 \square 5 - 72 \square 8 \\
&= 16 + 20 - 9 \\
&= 36 - 9 \\
&= 27
\end{aligned}$$

57. 2

57. $\begin{matrix} 5 & 3 & 2 & 1 & 6 & 4 & 8 & 1 & \boxed{2} \\ 3 & 4 & 5 & 6 & 8 & & & & \end{matrix}$

58. 2

58. 8 S 9 P 9 K 6

59. 2

59. 12 R 3 M 5 P 20
□ Total number of girls = 43

60. 3.

60. 1 970 1971 1972 1973 1974 1975 1976 1977 1978 1979 1980 1981
1 1 2 1 1 1 2 1 1 1 2
Same calendar repeats after 7 or multiple of 7 odd days, So 1981 will have same calendar as 1970.

61. 2

61. $\begin{matrix} 9 & 3 & 6 & 6 & 1 & 5 & 5 & 4 & 1 & \square \\ 1 & 7 & 5 & 2 & 8 & 4 & 4 & 9 & 3 & 6 & \square \\ \square & 8 & 2 & \square & 6 & 6 & 4 & 2 & \square & 3 & 1 & 2 \\ \square & 6 & 2 & 2 & & & & & & & & \end{matrix}$

62. 2

62. □□□□□
□□□□□
□□□□□
□□□□□
□ 4 □ 6 □ 9 □ 6 □ 2 □ 5
□ 4 □ 6 □ 9 □ 6 □ 2 □ 5
□ 2 3 □ 9 □ 12 □ 5 □ 2 □ 2
8 3 □ 3

= -

63. 1

63. As per observation

64. 4

64. As per observation

65. 1

65. As per observation

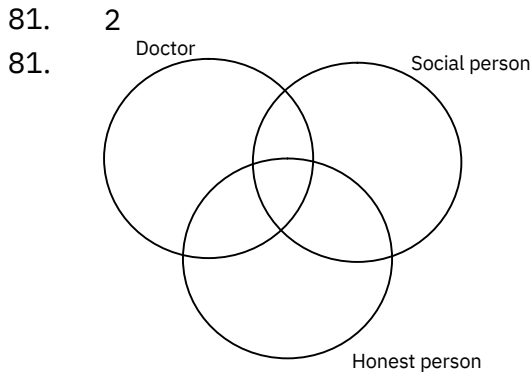
66. 3

66. As per observation
67. 1
 67. $132 \square 42 \square 153$
 $112 \square 12 \square 120$
 Similarly $62 \square 22 \square 32$
68. 2
 68. Total number of Biharis = $2 + 1 + 3 = 6$
69. 1
 69. Total number of Punjabis = $1 + 7 + 3 + 5 + 6 = 22$
70. 4
 70. Total number of Marathis = $3 + 6 + 4 + 8 = 21$
71. 2
 71. Only 2 Biharis are not Punjabis.
72. 4
 72. Punjabis who are not Marathis = $5 + 1 + 7 = 13$
73. 3
 73. 1949 26th Jan
 $1600 + 300 + 12LY + 37NLY$ 26
 $0 + 1 + 24 + 37$ 5
 62
 6
 \square Total number of odd days = 11
 = 4
 \square 26th Jan 1950 was Thursday
74. 1
 74. $12 \square 30 \square 48 \square 5.5 \square 96$
 \square Larger angle = $360 - 96$
 = 264
75. 2
 75. $23 \frac{40}{60}$ hrs of faulty clock = 24 hrs of actual clock
 or $\frac{71}{3}$ hrs of faulty clock = 24 hrs of actual clock
 \square 71 hrs of faulty clock = $\frac{24 \square 71}{71} \square 3$
 = 72 hrs of actual clock
 \square Correct time = 4 am
76. 3
 76. Clearly 2 & 5 are opposite
 1 & 6 are opposite
 4 & 3 are opposite
77. 3
 77. Here, $\square = 4$
 Clearly corner (8) cubes are 3 face coloured.
-

78. 4
 78. $12(n - 2) = 24$

79. 2
 79. $6(n - 2)2 = 24$

80. 3
 80. $4 \times 7 = 28$
 $3 \times 15 = 45$
 Similarly $2 \times 5 = 10$
 Logic of letter □ In every row A, B & C are present.



82. 2
 82. (1) Difference between B & Q = 15.
 (2) Difference between D & Y = 21.
 (3) Difference between U & F = 15
 (4) Difference between V & E = 17

83. 3
 83. In given sequence PO & in alphabetical order it is OP.

84. 4
 84. In given series letters between Y & L are 12 which is same as original alphabetical order & letters between L and F are 5 which is same as original alphabetical order.

85. 1
 85. A⁻ B⁻
Clearly B is the aunt of S.
 Daughter R⁺ B⁺

86. No option correct
 86. Sohan and Neeraj have no mentioned correlation with Abhay, Neena & Sunita.

87. $3 \ 18 - 10 = 8 \ 18 - 4$
 $= 14 \ 10 - 4 = 6$
 87. Similarly $15 - 5 = 10$

88. 2
 88. As per observation.

89. 1

89. As per observation.

90. 3

90. Horizontal lines = 3

Vertical lines = 5

Other lines = 8

Total number of lines required = 16

91. 3

91. Here, $n = 4$.

□ Cubes with no surface coloured = $(n - 2)^3 = 8$

92. 3

92. At least 2 face coloured = 2 face coloured + 3 face coloured
= $12(n - 2)^2 + 8 = 24 + 8 = 32$

93. 1

93. 2 surface painted red = $12(n - 2) = 24$

94. No option correct

94. 3 surface painted with red = corner cubes which are 8 in number.

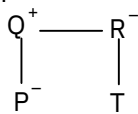
95. 3

95. Number of cubes obtained along each axis = 3

□ Total number of cubes = $3 \times 3 \times 3 = 27$

96. 4

96.



X □ Father

+ □ Daughter

□ □ Mother

- □ Brother

Clearly T is the cousin of P.

97. 4

97. (i)

P⁺

(ii)

P⁻

R⁺

Q

R⁺

Q⁺

T

T-

(iii)

P⁻

T⁺

(iv)

P⁺

R⁻

R⁺

Q⁻

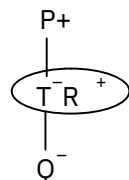
T⁺

Q⁻

98. 3

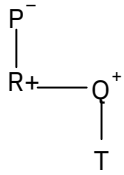
98.

Clearly R is the son in law of P.



99. 1

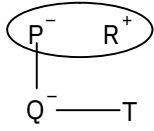
99.



Clearly P is the grand mother of T.

100.
100.

2



Clearly Q is the sister of T.

NTSE STAGE – I (DELHI STATE)
 05 – A (2019 – 20)
 (For Class – X)
 SCHOLASTIC APTITUDE TEST
 ANSWER KEYS

PHYSICS

101	2	102	4	103.	1	104	2
105.	3	106.	1	107.	4	108.	1
109.	2	110.	1	111	1	112	4
113	2						

CHEMISTRY

114	1, 2 & 4	115.	1	116.	3	117.	4
118.	12	119.	2	120.	4	121	1
122	1	123	4	124	1	125.	1
126.							

BIOLOGY

127.	3	128.	4	129.	1	130.	2
131	4	132	1	133	1	134	3
135.	2	136.	2	137.	4	138.	4
139.	1	140.	2				

MATHEMATICS

141.	1	142.	4	143.	4	144.	1
145.	4	146.	2	147.	3	148.	2
149.	3	150.	*	151.	3	152.	4
153.	1	154.	1	155.	4	156.	1
157.	1	158.	2	159.	4	160.	4

SOCIAL SCIENCE

161	4	162	1	163.	2 2 2	164.	4
165.	4	166.	2	167.	3 2 1 2	168.	3
169.	1	170.	3	171.	3 1 or	172.	3
173	2	174	3	175.	4	176.	1
177.	2	178.	3	179.	2	180.	4
181	3	182	3	183.		184.	3
185.	4	186.	4	187.		188.	4
189.	2	190.	3	191.		192.	4
193	2	194	1	195.		196.	4
197.	4	198.	2	199.		200.	1

Observations:

150. No option is correct. Correct answer is 198.2 Here, if the money means cash, then answer

195. would be (4), other wise answer would be (1), but as it is not clear in the question, answer should be either (1) or (4) or bonus should be given owing the error in the question.

NTSE STAGE – I (DELHI STATE)
 05 – A (2019 – 20)
 (For Class – X)
 SCHOLASTIC APTITUDE TEST
 HINTS & SOLUTIONS

101. 2

101. $P_i = 0$
 $P_f = 18 \times 6 + 12 V$
 $P_i = P_f$
 $V = 19 \text{ m/s}$

K.E. $= \frac{1}{2} \times 12 \times 9^2 = 6 \times 81 = 486 \text{ J}$

102. 4

102. Slope of $v - t$ graph gives acceleration and acceleration is constant from time $t = 0$ to $t = T$. After $t = T$, velocity is constant.

103. 1

103. $u = v = 40 \text{ cm}$
 $\frac{1}{v} = \frac{1}{u} + \frac{1}{f}$
 $\frac{1}{40} = \frac{1}{f}$
 $P = (2)5 \text{ D}$

104. 2

104. Convection is caused by gravity pulling heavier elements in a gas or liquid down.

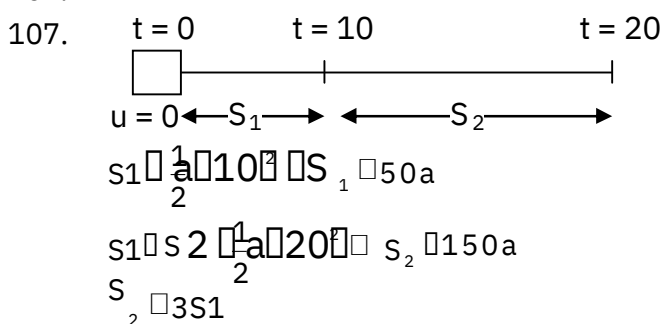
105. 3

105. $V_o = 4 \text{ m/s}$
 $V_I = 14 \text{ m/s}$
 $V_{Io} = V_I - V_o$
 $= 14 - 4 = 10 \text{ m/s}$

106. 1

106. $I = \frac{V}{R_{eq}}$
 $2 = \frac{6}{R}$
 $R = 3 \Omega$

107. 4



108. 1

108. $g = \frac{4}{3} G \rho R$

$$\frac{g_1}{r_1} = \frac{g_2}{r_2}$$

109. $\frac{g}{2}$

109. $f = 15 \text{ cm}$ $m = \frac{v}{u} = 2$

$$v = 2u$$

$$\frac{1}{v} = \frac{1}{u} + \frac{1}{f}$$

$$\frac{1}{2u} = \frac{1}{u} + \frac{1}{15}$$

$$u = 7.5 \text{ cm}$$

110. 1

110. $\frac{1}{4} = \frac{1}{2} g \sin \theta$... (i)

$\frac{1}{2} = \frac{1}{2} g \sin \theta$... (ii)

$$\frac{t^2}{4} = 4$$

$$t = 4 \text{ sec.}$$

111. 1

111. $P = \frac{V^2}{R}$

$$r \quad r \quad r \quad r$$

$$r$$

$$10 \frac{V^2}{4r}$$

$$P_1 = 40 \text{ W}$$

$$P_1 \frac{V^2}{r}$$

112. 4

112. $F = qVB \sin \theta$
If V is parallel to B $\theta = 0^\circ$
 $F = 0$

113. 2

113. $I = \frac{5}{50} = \frac{1}{10} \text{ A}$

$$5 \frac{100R}{100R}$$

$$R = 100 \Omega$$

114. 1, 2 & 4

- 114. Epsom salt ($\text{MgSO}_4 \cdot 7\text{H}_2\text{O}$)
- Green vitriol ($\text{FeSO}_4 \cdot 7\text{H}_2\text{O}$)
- White vitriol ($\text{ZnSO}_4 \cdot 7\text{H}_2\text{O}$)

115. 1
 115. Element Zn & Sn are used for galvanization.

116. 3
 116. $Zn \xrightarrow[A]{} CuSO_4 \xrightarrow[M]{} ZnSO_4 \xrightarrow[N]{} Cu$

117. 4
 117. Hydrogen has highest calorific value.

118. 1
 118. pH of acid rain is less than 5.6

119. 2
 119.
$$\begin{array}{ccccccc} & & O & & & & \\ & & || & & & & \\ CH_3 & - & C & - & CH_2 & - & CH_2 & - & CH_2 & - & COOH \\ 6 & & 5 & & 4 & & 3 & & 2 & & 1 \end{array}$$
 5-Keto hexanoic acid

120. 4
 120. $2 NaCl \xrightarrow{aq} 2 NaOH \xrightarrow{aq} H_2O$

121. 1
 121. $2KMnO_4 + 3H_2SO_4 \rightarrow K_2SO_4 + 2MnSO_4 + 3H_2O + 5O_2$

122. 2
 122.
$$\begin{array}{c} H \\ | \\ H - C - C - H \\ | \quad | \\ H \quad H \\ | \\ H \end{array}$$
 15 Covalent bond

123. 4
 123. No. of moles = $\frac{1000 \text{ g}}{56 \text{ g}} = 17.8 \text{ moles}$
 1 mole contains N_A atom of Fe
 So, 17.8 mole contain
 $17.8 \times 6.022 \times 10^{23} = 1.075 \times 10^{25}$ atoms

124. 1
 124. Alkali metal oxide are basic in nature.

125. 1
 125. The pH value of solution will be 7 to 9.

126. 1
 126. No. of valence electron will remain same for any group element.

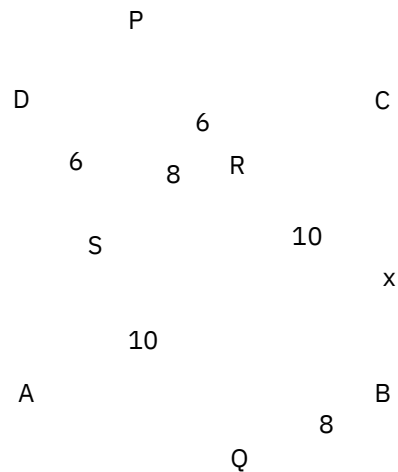
127. 3
 127. Oxidation-reduction reactions takes place during break down of molecules in the respiration in our body. Oxidation of glucose and reduction of oxygen.

128. 4
128. Lactic acid is produced when pyruvate is broken down in absence of oxygen in muscle cell.
129. 1 Separation of oxygenated deoxygenated blood allows a highly efficient supply of oxygen to the body, also useful in animals that have high energy needs such as birds and mammals which constantly use energy to maintain their body temperature.
130. 2
130. Root pressure is effective way transporting water in xylem during night.
131. 4
131. A Growth hormone
B Growth hormone releasing factor
C Insulin
D Thyroxine
132. 1
132. Wrinkled seed = rr
Heterozygous tall plant = Tt
- | | | |
|------|------|------|
| rrTt | X | rrTt |
| | rT | rt |
| rT | rTrT | rTrt |
| rt | rTrt | rtrt |
- rTrT – Homozygous wrinkled seed Homozygous tall
rTrt – Homozygous wrinkled heterozygous tall
rtrt – Homozygous wrinkled homozygous dwarf
100% Homozygous wrinkled
75% plants will be Tall and have wrinkled seed and 25% will be dwarf with wrinkled seed.
133. 1
133. Two similar pea plants are growing in two different islands separated by vast ocean. The phenomenon of geographical isolation will not be seen as the plants get self pollinated.
134. 3
134. DDT is non-biodegradable when it enters in food chain it gets accumulated in each trophic level. This phenomenon is called Biomagnification.
135. 2
135. Presence of coliform bacteria is an indicator of pollution level in water
136. 2
136. Leaves of tendu are the source of income of large number of people of India. These leaves are used to make bidis.
137. 4
137. Maximum number of trophic levels supported in any ecosystem is four.
138. 4
138. Correct sequence of reflex arc is
Receptor → Sensory Neuron → Relay Neuron → Motor Neuron → Effector organ

139. 1
 139. Tricuspid valve is present in right atrium and right ventricle

140. 2
 140. BCG vaccine provide protection against TB.

141. 1
 141. Extend BR and drawn DP BR on extended part.
 Extend DS and draw BQ DS on extended part then DPBQ is rectangle having sides 8 m and 16 m
 Diagonal of rectangle $= 8\sqrt{5}$
 If x is side of square then
 $2x^2 = 320 \Rightarrow x^2 = 160 \Rightarrow x = 4\sqrt{10}$



142. 4
 142. $2^x \cdot 4^3 = 4^x \cdot 2^3 = 4^x \cdot 2^x \cdot 6^3$
 $\Rightarrow 2^x \cdot 4^3 = 4^x \cdot 2^3 = 6 \cdot 4^x \cdot 2^x \cdot 6^3$

Now $2^x \cdot 4^3 = 4^x \cdot 2^3 = 6 \cdot 4^x \cdot 2^x \cdot 6^3$
 $\Rightarrow 2^x \cdot 4^3 = 4^x \cdot 2^3 = 6 \cdot 4^x \cdot 2^x \cdot 6^3$
 $\Rightarrow 3 \cdot 2^x = 4^x \cdot 6^3$
 Now $2^x \cdot 4^3 = 0 \Rightarrow 2^x = 0$
 $4^x \cdot 2^3 = 0 \Rightarrow x = \frac{1}{2}$
 $6 \cdot 4^x \cdot 2^x = 0 \Rightarrow 2^x \cdot 3 \cdot 2^x \cdot 2^x = 0$
 $\Rightarrow 2^x \cdot 2^x = 0$ or $2^x \cdot 3 = 0$
 $\Rightarrow 2^x = 2$ or $2^x = 3$ (Not possible)
 $\Rightarrow x = 1$

So sum of all real values of
 $x = 2 \cdot \frac{1}{2} + 1 = 2$

143. 4
 143. Let $2019x = y$ then given question reduces to $y = \frac{1}{y} = 3$

$\Rightarrow y^3 = \frac{1}{y^3} = 18$ and $y^2 = \frac{1}{y^2} = 7$
 Now $\sqrt{\frac{20196x \cdot 2019^{6x}}{2019x \cdot 2019^x}} = \sqrt{\frac{y^6 \cdot \frac{1}{y}}{y \cdot \frac{6}{1}}}$
 y

$$\sqrt{\frac{1}{y} - \frac{1}{y^2} + \frac{1}{y^3} - \frac{1}{y^4}} = \sqrt{144} = 12$$

144. 1

144. Since p is root of $x^2 - 5x + 7 = 0$

$$p^2 - 5p + 7 = 0$$

$$p^2 - 5p = -7$$

Now radius of circle

$$r = \sqrt{p^2 - 4p + 4}$$

$$= \sqrt{2p - 5p + 7} = \sqrt{3} \text{ units}$$

$$\text{Area of circle} = 3 \text{ sq. units}$$

145. 4

$$145. \frac{1}{x^2y} - \frac{1}{x} + \frac{1}{y} = 2 \quad \Rightarrow y^2 - xy = 0$$

Dividing both sides by y^2 we get

$$\frac{x^2}{y} - \frac{x}{y} + \frac{1}{y} = 2$$

$$\text{Let } \frac{x}{y} = k \text{ then } k^2 - k + 1 = 0$$

$$\text{Now } \frac{x^6}{y^6} - \frac{x^3}{y^3} = k^6 - k^3$$

$$\text{Since } k^6 - k^3 = k^2 - k + 1 \Rightarrow k^4 - k^3 = 2k^2 - 2$$

$$k^4 - k^3 = 2 \quad (\text{since } k^2 - k + 1 = 0)$$

146. 2

$$146. x^3 - 597x^2 + 5236x = 0$$

$$\text{Sum of roots} = a + b + c = 0$$

$$\text{Also, } abc = 5236$$

$$\text{Since } a + b + c = 0$$

$$a^3 + b^3 + c^3 = 3abc$$

$$= 15708$$

147. 3

$$147. \cos \operatorname{cosec} x = \cot x = a$$

$$\operatorname{cosec} x = \cot x = \frac{1}{a}$$

On adding both equations

$$\operatorname{cosec} x = \frac{a^2 + 1}{2a} \quad \cos x = \frac{a - 1}{2}$$

$$a$$

148. 2

$$148. \text{Mean} = \frac{a^{15} + a^{16} + a^{136} + a^{137}}{4}$$

$$\frac{a^{14} + a^{15} + a^{135} + a^{136}}{4}$$

$$\frac{a^{75} + a^{75 \cdot 3} + a^{227}}{2}$$

149. 3

Using AM-GM

$$\frac{\tan^2 x + \cot^2 x}{2} \geq \sqrt{\tan^2 x \cot^2 x}$$

$$\tan^2 x + \cot^2 x \geq 2$$

So minimum value is 2.

150. No option is correct

$$f(x) = x^4 + ax^3 + bx^2 + cx + d$$

$$f(1) = 5, f(2) = 10, f(3) = 15, f(4) = 20$$

On the basis of given information

$$\text{Let } f(x) = x^5 + x^4 + x^3 + x^2 + x + 1 = 5x$$

$$f(12) = 7980, f(8) = 11840$$

$$\text{Now } \frac{f(12) - f(8)}{100} = 198.2$$

151. 3

Let numbers are $12x$ and $12y$, $\text{HCF}(x, y) = 1$

then $12x + 12y = 2160$

$$xy = 15 \cdot 5 \cdot 3$$

$$x = 5, y = 3$$

So, numbers are 60 and 36

$$\text{Sum} = 96$$

152. 4

Let angles are $x = 2d, x = d, x = d, x = 2d$ then $5x = 540^\circ$

$$x = 108^\circ$$

Sum of largest and smallest angle = $2x = 216^\circ$

153. 1

$$\sqrt{p} + q = 20$$

$$p = 20 - q \Rightarrow q^2 = 400 - 40q$$

$$p = 5q + 400 - q = 40q + 5q = 400 + 4q$$

$$400 + 4q = 10q$$

$$400 = 4q \Rightarrow q = 10, p = 25$$

$$400 + 100 = 4 \sqrt{q} + 5 \Rightarrow 500 = 4 \sqrt{q} + 5$$

$$p = 5q = 500$$

$$\frac{p + 5q}{100} = \frac{500 + 500}{100} = 5$$

154. 1

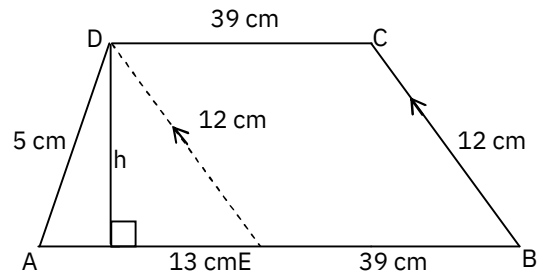
154. Draw DECB

□BCDE is a parallelogram

$$\text{ar} \square ADCE = 30 \text{ cm}^2$$

$$\frac{1}{2} \times 13 \times h = 30 \quad \square \quad h = \frac{60}{13} \text{ cm}$$

$$\text{ar} \square ABCD = \frac{1}{2} \times 52 \times 39 = \frac{60}{13} \times 39 = 210 \text{ cm}^2$$



155. 4

155. Among all triangles inscribed in a circle of given radius equilateral triangle has maximum area

Let side of □ABC = x

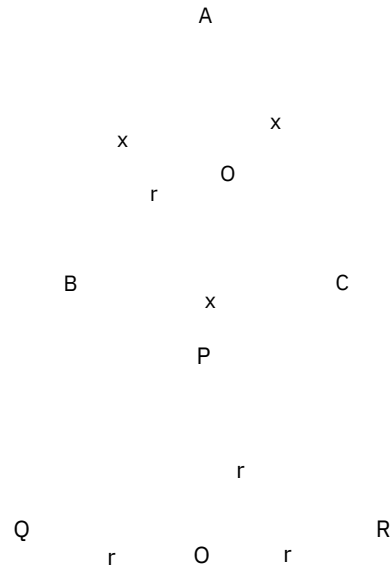
$$\text{then } r = \frac{x^3}{4 \times \frac{\sqrt{3}}{4} x^2}$$

$$\square \quad x = \sqrt{3}r$$

$$\text{Area of } \square ABC = \frac{\sqrt{3}}{4} \times x^2 = \frac{3\sqrt{3}}{4} r^2$$

When largest triangle is inscribed in a semicircle of radius r then base of □ = 2r, height of □ = r

$$\text{Area of } \square PQR = r^2$$



$$\text{Difference} = \frac{3\sqrt{3}}{4} r^2 - r^2 = \frac{3\sqrt{3}-4}{4} r^2$$

156. 1

156. Either of p or r is 2.

$$\text{Let } p = 2$$

$$q + r = 70$$

$$r + s = 72$$

$$q + 2r + s = 142$$

$$r = 142 - 89 = 53$$

$$\text{if } r = 2,$$

$$p + q = 70 \quad p + s$$

$$= 72 \quad q + s = 87$$

$$2p + q + s = 142$$

$$2p = 142 - 87 = 55$$

$$p = \frac{55}{2}, \text{ not possible}$$

157. 1

157. CE = 10 units.

□CFE ~ □CED

$$\square \frac{CF}{CE} = \frac{CE}{CD}$$

$$\frac{m}{10} - \frac{10}{15m} = m - 5$$

158. 2

158. Let $y = x^2 - 10x + 6$

$$\frac{1}{y-24} - \frac{1}{y-40} = \frac{9}{2}$$

$$y-24 = 64 \quad y-40 = 960$$

$$32y = 960$$

$$y = 30$$

$$x^2 - 10x + 6 = 30$$

$$x^2 - 13x + 3 = 0 \quad x = 13, 3$$

$$\text{Sum} = 13 - 3 = 10$$

159. 4

$$159. \quad N = \frac{2^{2/3} - 2^{1/3}}{2^{2/3} - 2^{1/3}} = \frac{2^{1/3} - 1}{2^{1/3} - 1} = 1$$

$$2^{1/3} - 1 = \frac{1}{N} \quad 2^{1/3} = \frac{1}{N} + 1$$

$$\left(\frac{1}{N} + 1\right)^3 = 2 \quad \frac{1}{N^3} + \frac{3}{N^2} + \frac{3}{N} + 1 = 2$$

$$\frac{1}{N^3} + \frac{3}{N^2} + \frac{3}{N} = 1$$

$$\frac{1}{N^3} + \frac{3}{N^2} + \frac{3}{N} - 1 = 0$$

160. 4

160. $x_1, x_2, \dots, x_n = pn \dots (i)$

$x_1, x_2, \dots, x_n = 10^q \dots (ii)$

$x_1, x_2, \dots, x_n = n \cdot 10^r \dots (iii)$

$$pn = 10^q \cdot n \cdot 10^r$$

$$n = \frac{10^q \cdot 10^r}{p}$$

$$n = \frac{10^{q+r}}{p}$$