

NTSE STAGE – I (DELHI STATE)
05 – A (2019 – 20)
(For Class – X)
SCHOLASTIC APTITUDE TEST
HINTS & SOLUTIONS

101. 2

101. $P_i = 0$
 $P_f = 18 \times 6 + 12 V$
 $P_i = P_f$
 $V = 9 \text{ m/s}$

K.E. $= \frac{1}{2} \times 12 \times 9^2 = 486 \text{ J}$

102. 4

102. Slope of $v - t$ graph gives acceleration and acceleration is constant from time $t = 0$ to $t = T$. After $t = T$, velocity is constant.

103. 1

103. $u = v = 40 \text{ cm}$
 $\frac{1}{v} = \frac{1}{u} + \frac{1}{f}$
 $\frac{1}{40} = \frac{1}{f}$
 $f = 40 \text{ D}$

104. 2

104. Convection is caused by gravity pulling heavier elements in a gas or liquid down.

105. 3

105. $V_o = 4 \text{ m/s}$
 $V_l = 8 \text{ m/s}$
 $V_{lo} = V_l - V_o$
 $= 8 - 4 = 4 \text{ m/s}$

106. 1

106. $I = \frac{V}{R_{eq}}$
 $2 = \frac{6}{R}$
 $R = 3 \Omega$

107. 4

107. $t = 0$ $t = 10$ $t = 20$

$u = 0$ $\leftarrow S_1 \rightarrow$ $\leftarrow S_2 \rightarrow$

$S_1 = \frac{1}{2} a \times 10^2 = 50a$

$S_1 = S_2 = \frac{1}{2} a \times 20^2 = 200a$

$S_2 = 3S_1$

108. 1
 108. $g \propto \frac{4}{3} G \rho R$

$$\frac{g_1}{r_1} = \frac{g_2}{r_2}$$

109. $\frac{g}{2}$

109. $f \propto \frac{1}{u} = 15 \text{ cm}$ $m \propto \frac{v}{u} = 2$

$$v \propto 2u$$

$$\frac{1}{v} \propto \frac{1}{u} \propto \frac{1}{f}$$

$$\frac{1}{2u} \propto \frac{1}{u} \propto \frac{1}{15}$$

$$u = 7.5 \text{ cm}$$

110. 1

110. $\frac{1}{4} \propto \frac{1}{2} g \sin \theta$... (i)

$\frac{1}{2} \propto \frac{1}{2} g \sin \theta$... (ii)

$$t^2 \propto 4$$

$$t = 4 \text{ sec.}$$

111. 1

111. $P \propto \frac{V^2}{R}$

$$r \quad r \quad r \quad r$$

$$r$$

$$10 \propto \frac{V^2}{4r}$$

$$P_1 = 40 \text{ W}$$

$$P_1 \propto \frac{V^2}{r}$$

112. 4

112. $F = qVB \sin \theta$
 If V is parallel to B $\theta = 0^\circ$
 $F = 0$

113. 2

113. $I \propto \frac{5}{50} \propto \frac{1}{10} \text{ A}$

$$5 \propto \frac{100R}{100R}$$

$$R = 100 \Omega$$

114. 1, 2 & 4

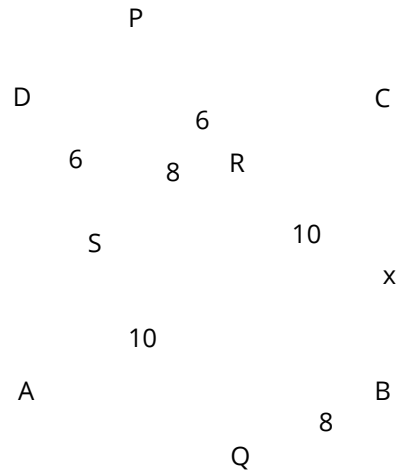
114. Epsom salt ($\text{MgSO}_4 \cdot 7\text{H}_2\text{O}$)
 Green vitriol ($\text{FeSO}_4 \cdot 7\text{H}_2\text{O}$)
 White vitriol ($\text{ZnSO}_4 \cdot 7\text{H}_2\text{O}$)

128. 4
128. Lactic acid is produced when pyruvate is broken down in absence of oxygen in muscle cell.
129. 1 Separation of oxygenated deoxygenated blood allows a highly efficient supply of oxygen to the body, also useful in animals that have high energy needs such as birds and mammals which constantly use energy to maintain their body temperature.
130. 2
130. Root pressure is effective way transporting water in xylem during night.
131. 4
131. A Growth hormone
B Growth hormone releasing factor
C Insulin
D Thyroxine
132. 1
132. Wrinkled seed = rr
Heterozygous tall plant = Tt
- | | | |
|------|------|------|
| rrTt | X | rrTt |
| | rT | rt |
| rT | rTrT | rTrt |
| rt | rTrt | rtrt |
- rTrT – Homozygous wrinkled seed Homozygous tall
rTrt – Homozygous wrinkled heterozygous tall
rtrt – Homozygous wrinkled homozygous dwarf
100% Homozygous wrinkled
75% plants will be Tall and have wrinkled seed and 25% will be dwarf with wrinkled seed.
133. 1
133. Two similar pea plants are growing in two different islands separated by vast ocean. The phenomenon of geographical isolation will not be seen as the plants get self pollinated.
134. 3
134. DDT is non-biodegradable when it enters in food chain it gets accumulated in each trophic level. This phenomenon is called Biomagnification.
135. 2
135. Presence of coliform bacteria is an indicator of pollution level in water
136. 2
136. Leaves of tendu are the source of income of large number of people of India. These leaves are used to make bidis.
137. 4
137. Maximum number of trophic levels supported in any ecosystem is four.
138. 4
138. Correct sequence of reflex arc is
Receptor → Sensory Neuron → Relay Neuron → Motor Neuron → Effector organ
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139. 1
 139. Tricuspid valve is present in right atrium and right ventricle

140. 2
 140. BCG vaccine provide protection against TB.

141. 1
 141. Extend BR and draw DP ⊥ BR on extended part.
 Extend DS and draw BQ ⊥ DS on extended part then DPBQ is rectangle having sides 8 m and 16 m
 Diagonal of rectangle $= 8\sqrt{5}$
 If x is side of square then
 $2x^2 = 320 \Rightarrow x^2 = 160 \Rightarrow x = 160m^2$



142. 4
 142. $2^x \cdot 4^3 \cdot 4^x \cdot 2^3 \cdot 4^x \cdot 2^x \cdot 6^3$
 $= 2^x \cdot 4^3 \cdot 4^x \cdot 2^3 \cdot 6 \cdot 4^x \cdot 2^x \cdot 6^3$

Now $2^x \cdot 4^3 \cdot 4^x \cdot 2^3 \cdot 6 \cdot 4^x \cdot 2^x \cdot 6^3$

$= 2^x \cdot 4^3 \cdot 4^x \cdot 2^3 \cdot 6 \cdot 4^x \cdot 2^x \cdot 6^3$

$= 3 \cdot 2^x \cdot 4^x \cdot 4^x \cdot 2^x \cdot 6^3$

Now $2^x \cdot 4^x \cdot 4^x \cdot 2^x \cdot 6^3$

$4^x \cdot 2^x \cdot 0 \cdot x \cdot \frac{1}{2}$

$6 \cdot 4^x \cdot 2^x \cdot 0 \cdot 2^x \cdot 3 \cdot 2^x \cdot 2 \cdot 0$

$2^x \cdot 2 \cdot 0$ or $2^x \cdot 3 \cdot 0$

$2^x \cdot 2$ or $2^x \cdot 3$ (Not possible)

$x = 1$

So sum of all real values of

$$x = 2 \cdot \frac{1}{2} + 1 \cdot \frac{7}{2} = 3.5$$

143. 4

143. Let $2019x = y$ then given question reduces to $y^{\frac{1}{y}} = 3$

$$y^3 = \frac{1}{y^3} = 18 \text{ and } y^2 = \frac{1}{y^2} = 7$$

$$\text{Now } \sqrt{\frac{20196x \cdot 2019^{6x}}{2019x \cdot 2019^x}} = \sqrt{\frac{y^6 \cdot \frac{1}{y}}{y \cdot \frac{6}{1}}}$$

$$y$$

$$\sqrt{\frac{1}{y} - \frac{1}{y^2} + \frac{1}{y^3} - \frac{1}{y^4} + \frac{1}{y^5} - \frac{1}{y^6} + \frac{1}{y^7} - \frac{1}{y^8} + \frac{1}{y^9} - \frac{1}{y^{10}} + \frac{1}{y^{11}} - \frac{1}{y^{12}}}$$

144. 1

144. Since p is root of $x^2 - 5x + 7 = 0$
 $p^2 - 5p + 7 = 0$
 $p^2 - 5p = -7$

Now radius of circle

$$r = \sqrt{p^2 + 1 + p^2 + 4}$$

$$= \sqrt{2 + 2p + 7} = \sqrt{3} \text{ units}$$

Area of circle = 3π units

145. 4

145. $\frac{1}{x^2 y} - \frac{1}{x} + \frac{1}{y} = x^2 - y^2 - xy = 0$

Dividing both sides by y^2 we get

$$\frac{x^2}{y} - \frac{x}{y} + \frac{1}{y} = x^2 - y^2 - xy = 0$$

Let $\frac{x}{y} = k$ then $k^2 - k + 1 = 0$

Now $\frac{x^6}{y^6} - \frac{x^3}{y^3} = k^6 - k^3$

Since $k^6 - k^3 = k^2 - k + 1 \cdot k^4 - k^3 + 2k^2 - 2$

$= k^4 - k^3 + 2$ (since $k^2 - k + 1 = 0$)

146. 2

146. $x^3 - 597x + 5236 = 0$

Sum of roots = $a + b + c = 0$

Also, $abc = 5236$

Since $a + b + c = 0$

$$a^3 + b^3 + c^3 = 3abc$$

$$= 15708$$

147. 3

147. $\cos \operatorname{cosec} x = \cot x = a$

$$\operatorname{cosec} x = \cot x = \frac{1}{a}$$

On adding both equations

$$\operatorname{cosec} x = \frac{a^2 + 1}{2a} \quad \cos x = \frac{a + 1}{a}$$

148. 2

148. Mean = $\frac{a^{15} + a^{16} + a^{136} + a^{137}}{4}$

$$\frac{a^{14} + a^{15} + a^{16} + a^{17} + a^{18} + a^{19} + a^{20}}{4}$$

$$a^{17.5} = a^{17} \cdot a^{0.5}$$

$$2 \cdot 75 \cdot 3 = 227$$

149. 3

Using AM \geq GM

$$\frac{\tan^2 x + \cot^2 x}{2} \geq \sqrt{\tan^2 x \cot^2 x}$$

$$\tan^2 x + \cot^2 x \geq 2$$

So minimum value is 2.

150. No option is correct

$$f(x) = x^4 + ax^3 + bx^2 + cx + d$$

150.

$$f(1) = 5, f(2) = 10, f(3) = 15, f(4) = 20$$

On the basis of given information

$$\text{Let } f(x) = x^4 + ax^3 + bx^2 + cx + d$$

$$f(1) = 12 = 1 + a + b + c + d$$

$$\text{Now } \frac{f(1) + f(2) + f(3) + f(4)}{4} = 198.2$$

151. 3

Let numbers are $12x$ and $12y$, $\text{HCF}(x, y) = 1$

151.

$$\text{then } 12x + 12y = 2160$$

$$xy = 15 \cdot 5 \cdot 3$$

$$x = 5, y = 3$$

So, numbers are 60 and 36

$$\text{Sum} = 96$$

152. 4

Let angles are $x = 2d, x = d, x = d, x = 2d$ then $5x = 540^\circ$

152.

$$x = 108^\circ$$

Sum of largest and smallest angle $= 2x = 216^\circ$

153. 1

$$\sqrt{p} + q = 20$$

153.

$$p = 20 - q \Rightarrow q^2 = 400 - 40q$$

$$p = 5q + 400 - q = 40q + 400$$

$$p = 400 + 4q = 10q$$

$$400 + 4q = 10q \Rightarrow 25q = 400$$

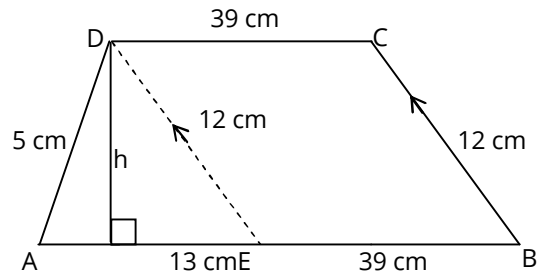
$$q = 100 \Rightarrow 4\sqrt{q} = 5 \Rightarrow 500 = 4\sqrt{q} = 5^2$$

$$p = 5q = 500$$

$$\frac{p}{100} = \frac{5q}{100} = \frac{500}{100} = 5$$

154. 1

154. Draw DECB
 BCDE is a parallelogram
 $\text{ar} \square ADE = 30 \text{ cm}^2$
 $\frac{1}{2} \times 13 \times h = 30 \Rightarrow h = \frac{60}{13} \text{ cm}$
 $\text{ar} \square ABCD = \frac{1}{2} \times 39 \times \frac{60}{13} = 210 \text{ cm}^2$



155. 4
 155. Among all triangles inscribed in a circle of given radius equilateral triangle has maximum area

Let side of $\square ABC = x$

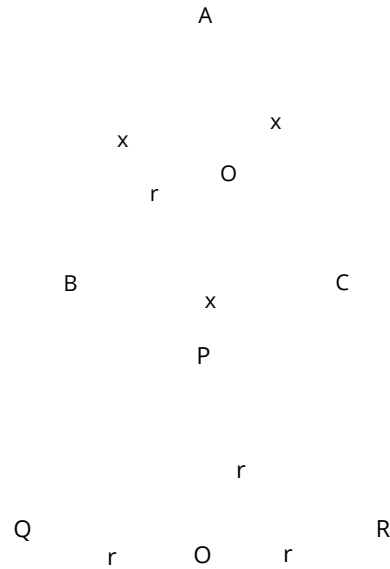
$$\text{then } r = \frac{x^3}{4 \times \frac{\sqrt{3}}{4} x^2}$$

$$\Rightarrow x = \sqrt{3}r$$

$$\text{Area of } \square ABC = \frac{\sqrt{3}}{4} \times x^2 = \frac{3\sqrt{3}}{4} r^2$$

When largest triangle is inscribed in a semicircle of radius r then base of $\square = 2r$, height of $\square = r$

$$\text{Area of } \square PQR = r^2$$



$$\text{Difference} = \frac{3\sqrt{3}}{4} r^2 - r^2 = \frac{3\sqrt{3}-4}{4} r^2$$

156. 1
 156. Either of p or r is 2.

$$\begin{aligned} \text{Let } p &= 2 \\ q + r &= 70 \\ r + s &= 72 \\ q + 2r + s &= 142 \\ r &= 142 - 89 = 53 \end{aligned}$$

$$\begin{aligned} \text{if } r &= 2, \\ p + q &= 70 \quad p + s \\ &= 72 \quad q + s = 87 \\ 2p + q + s &= 142 \end{aligned}$$

$$2p = 142 - 87 = 55$$

$$p = \frac{55}{2}, \text{ not possible}$$

157. 1
 157. CE = 10 units.

$$\square CFE \sim \square CED$$

$$\frac{CE}{FE} = \frac{CE}{ED}$$

$$\frac{m}{10} = \frac{10}{15m} = m = 5$$

158. 2

158. Let $y = x^2 = 10x = 6$

$$y = 24 \quad y = 40 \quad y = 9$$

$$y = 2y^6 = 2y^2 = 4y = 960$$

$$32y = 960$$

$$y = 30$$

$$x = 10x = 69 = 30$$

$$x = 13 = x = 3 = 10 = 13, 3$$

$$\text{Sum} = 13 - 3 = 10$$

159. 4

$$159. \quad N = \frac{2^{2/3} \cdot 2^{1/3} \cdot 2^{1/3} \cdot 2^{1/3}}{2^{2/3} \cdot 2^{1/3} \cdot 2^{1/3} \cdot 2^{1/3}}$$

$$2^{1/3} \cdot \frac{1}{N} = 2^{1/3} \cdot \frac{1}{N} = 1$$

$$\frac{2^{1/3}}{N} = \frac{1}{N} \cdot \frac{1}{N} = \frac{1}{N^2} = \frac{1}{N^3} = \frac{1}{N^2} = \frac{1}{N^3}$$

$$2 = \frac{1}{N^3} = \frac{1}{N^2} = \frac{1}{N^3}$$

$$\frac{1}{N^3} = \frac{3}{N^2} = \frac{3}{N}$$

160. 4

160. $x_1 = x_2 = \dots = x_n = pn \dots (i)$

$x_1 = x_2 = \dots = x_{10} = 10q \dots (ii)$

$x_{11} = x_{12} = \dots = x_n = n = 10r \dots (iii)$

$$pn = 10q = r = n = 10$$

$$n = \frac{10q}{p} = r$$