### JEE(Main)-2024 | 04 April 2024 (Shift-1 Morning) | Question Paper with Solutions | Memory Based

#### **MATHEMATICS**

1. If 
$$f(x) = \begin{cases} x-2 & 0 \le x \le 2 \\ -2 & -2 \le x \le 0 \end{cases}$$
 and  $h(x) = f(|x|) + |f(x)|$  then  $\int_{0}^{k} h(x) dx$  is equal to  $(k > 0)$ 

- (1) 0
- (2)  $\frac{k}{2}$
- (3) 2k
- (4) k

**Ans.** (1)

**Sol.** 
$$f(|x|) = \begin{cases} -2 - x, & x < 0 \\ x - 2, & x > 0 \end{cases} |f(x)| = \begin{cases} 2, x < 0 \\ 2 - x, & x > 0 \end{cases}$$
$$\Rightarrow h(x) = f(|x|) + |f(x)| = \begin{cases} -x, & x < 0 \\ 0, & x > 0 \end{cases}$$
$$\Rightarrow \int_0^x h(x) dx = \int_0^x 0 dx = 0$$

- 2. There are three bags A, B and C. Bag A contain 7 Black balls and 5 Red balls, Bag B contains 5 Red and 7 Black balls and Bag C contain 7 Red and 7 Black balls. A ball is drawn and found to be black find probability that it is drawn from Bag A.
- **Ans.**  $(\frac{7}{18})$

Sol.

$$Prob = \frac{\frac{7}{12}}{\frac{7}{12} + \frac{5}{12} + \frac{7}{14}}$$

$$= \frac{\frac{7}{6}}{\frac{7}{6} + \frac{5}{6} + 1}$$
$$= \frac{7}{7 + 5 + 6} = \frac{7}{18}$$

3. Find the number of rational numbers in the expansion of  $\left(2^{\frac{1}{5}} + 5^{\frac{1}{3}}\right)^{15}$ .

**Ans.** (2

**Sol.** 
$$T_{r+1} = {}^{15}C_r (2^{1/5})^{15-r} (5^{1/3})^r$$
  
=  ${}^{15}C_r 2^{3-\frac{r}{5}}.5^{\frac{r}{3}}; r = 3K \& 5K$ 

There r = 0; 15

So Total No. of Rational Terms are "2".

4. Find value of 
$$\int_{0}^{\frac{\pi}{2}} \frac{\sin^2 x}{1 + \sin x \cos x} dx$$

Ans. 
$$(\frac{\pi}{3\sqrt{3}})$$

**Sol.** 
$$\Rightarrow | = \int_0^{\pi/2} \frac{\cos^2 x dx}{1 + \sin x \cos x}$$

$$\therefore 2I = \int_0^{\pi/2} \frac{2dx}{2 + \sin 2x}$$

$$I = \int_0^{\pi/2} \frac{dx}{2 + \frac{2 \tan x}{1 + \tan^2 x}}$$

$$2I = \int_0^{\pi/2} \frac{\sec^2 x dx}{\tan^2 x + \tan x + 1}$$

$$2I = \int_0^\infty \frac{dt}{t^2 + t + 1}$$

$$2I = \int_0^\infty \frac{dt}{\left(t + \frac{1}{2}\right)^2 + \left(\frac{\sqrt{3}}{2}\right)^2}$$

$$2I = \frac{1}{\sqrt{3}/2} \left[ tan^{-1} \left( \frac{t + \frac{1}{2}}{\sqrt{3}/2} \right) \right]_{0}^{\infty}$$

$$I = \frac{1}{\sqrt{3}} \left[ \frac{\pi}{2} - \frac{\pi}{6} \right]$$

$$I = \frac{\pi}{3\sqrt{3}}$$

5. If 
$$x^2 - ax + b = 0$$
 has roots 2, 6; and  $\alpha = \frac{1}{2a+1}$ ;  $\beta = \frac{1}{2b-a}$ . Find equation having roots  $\alpha$ ,  $\beta$ .

**Ans.** 
$$(272x^2 - 33x + 1 = 0)$$

**Sol.** 
$$a = 2 + 6 = 8$$

$$b = 2 \times 6 = 12$$

$$\alpha = \frac{1}{17}; \beta = \frac{1}{16}$$

Required EQ<sup>n</sup> = 
$$x^2 - \left(\frac{1}{17} + \frac{1}{16}\right)x + \frac{1}{17} \times \frac{1}{16}$$

$$\Rightarrow 272x^2 - 33x + 1 = 0$$

6. 
$$\lim_{x \to 4} \frac{\left(5 + x\right)^{\frac{1}{3}} - \left(1 + 2x\right)^{\frac{1}{3}}}{\left(5 + x\right)^{\frac{1}{2}} - \left(1 + 2x\right)^{\frac{1}{2}}}$$

Ans. 
$$(\frac{2 \times 9^{1/3}}{9})$$

**Sol.** 
$$\lim_{x \to 4} \frac{(5+x)^{1/3} - (1+2x)^{1/3}}{(5+x)^{1/2} - (1+2x)^{1/2}}$$

$$\frac{(9+h)^{1/3} - (9+2h)^{1/3}}{(9+h)^{1/2} - (9+2h)^{1/2}} = \frac{9^{1/3} \left[ \frac{h}{27} - \frac{2h}{27} \right]}{3 \left( \frac{h}{18} - \frac{h}{9} \right)}$$

$$=\frac{9^{1/3}}{3}\frac{\left(\frac{-h}{27}\right)}{\frac{-h}{18}}$$

$$=\frac{2\times 9^{1/3}}{9}$$

**7.** AB, BC, CA are sides of triangle having 5, 6, 7 points respectively. How many triangles are possible using these points.

**Ans.** (751)

**Sol.** 
$$^{18}$$
  $c_3 - ^5$   $c_3 - ^6$   $c_3 - ^7$   $c_3$   
= 17 × 16 × 3 - 10 - 20 - 35  
= 816 - 65 = 751

**8.** 2, p and q are in G.P. in an A.P. 2 is third term, p is 7<sup>th</sup> term and q is 8<sup>th</sup> term find p and q.

**Ans.** 
$$(P = \frac{1}{2}, q = \frac{1}{8})$$

**Sol.** 
$$p = 2r, q = 2r^2$$

$$A + 2d = 2$$

$$A + 6d = 2r$$

$$A + 7d = 2r^2$$

By Solving 
$$r = \frac{1}{4}$$

$$P = \frac{1}{2}, q = \frac{1}{8}$$

9. If the domain of the function  $\sin^{-1}\left(\frac{3x-22}{2x-19}\right) + \log_{e}\left(\frac{3x^2-8x+5}{x^2-3x-10}\right)$  is  $[\alpha, \beta]$  then  $3\alpha + 10\beta$  is equal to

**Ans.** (3)

**Sol.** 
$$-1 \le \frac{3x-22}{2x-19} \le 1$$

$$\frac{3x-22}{2x-19}+1\geq 0$$

$$\frac{5x-41}{2x-19} \ge 0 \Rightarrow x \in \left(-\infty, \frac{41}{5}\right] \cup \left(\frac{19}{2}, \infty\right)$$

$$\frac{3x-22}{2x-19} - 1 \le 0$$

$$\frac{x-3}{2x-19} \le 0 \Longrightarrow x \in \left[3, \frac{19}{2}\right)$$

$$\frac{+}{3}$$
  $\frac{-}{19}$ 

$$\frac{3x^2 - 3x - 5x + 5}{x^2 - 5x + 2x - 10} > 0$$

$$\frac{(3x-5)(x-1)}{(x-5)(x+2)} > 0$$

$$\Rightarrow \left[5, \frac{41}{5}\right]$$

$$=3\times5+10\times\frac{41}{5}$$

**10.** 
$$x + (2\sin 2\theta) y + 2\cos 2\theta = 0$$

$$x + (\sin\theta) y + \cos\theta = 0$$

$$x + (\cos\theta) y - \sin\theta = 0$$

find nontrivial solution

Ans. 
$$(\alpha = \cos^{-1}\left(\frac{1}{2\sqrt{2}}\right))$$

Sol. 
$$\begin{vmatrix} 1 & 2\sin 2\theta & 2\cos \theta \\ 1 & \sin \theta & \cos \theta \end{vmatrix} =$$

$$\begin{vmatrix} 1 & \sin\theta & \cos\theta \\ 1 & \cos\theta & -\sin\theta \end{vmatrix} = 0$$

$$1\left[-\sin^2\theta-\cos^2\theta\right]-2\sin2\theta\left[-\sin\theta-\cos\theta\right]+2\cos2\theta\left[\cos\theta-\sin\theta\right]=0$$

$$-1+2\sin 2\theta(\sin\theta+\cos\theta]+2\cos 2\theta[\cos\theta-\sin\theta]=0$$

$$-1 + 2\sin\theta\sin2\theta + 2\sin2\theta\cos\theta + 2\cos\theta\cos2\theta - 2\cos2\theta\sin\theta = 0$$

$$-1+2\cos\theta+2\sin\theta=0$$

$$\sin\theta + \cos\theta = \frac{1}{2}$$

$$\frac{1}{\sqrt{2}}\sin\theta + \frac{1}{\sqrt{2}}\cos\theta = \frac{1}{2\sqrt{2}}$$

$$\cos\left(\theta - \frac{\pi}{4}\right) = \cos\alpha$$

$$\theta - \frac{\pi}{4} = 2n\pi \pm \alpha$$

where 
$$\alpha = \cos^{-1}\left(\frac{1}{2\sqrt{2}}\right)$$

Let  $f(x) = x^5 + 2e^{x/4}$  for all  $x \in R$ . consider a function (gof)(x) = x for all  $x \in R$ . Then the value 11. of 8g'(2) is

(2) Ans.

**Sol.** 
$$g(f(x)) = x$$

$$g'(f(x)).f'(x) = 1$$

$$g'(f(x)) = \frac{1}{f'(x)}$$
;

$$f'(x) = 5x^4 + \frac{1}{2}e^{x/4}$$

$$g'(2) = \frac{1}{f'(0)} = \frac{1}{2/4} = 2$$

$$f'(0) = \frac{1}{2}$$

$$8'g'(2) = 16$$

Let  $f(x) = \frac{2x^2 - 3x + 9}{2x^2 + 3x + 4}$ . If maximum value of f(x) is m and minimum value of f(x) is n then 12. find

m + n? Ans. (10)

**Sol.** 
$$y = \frac{2x^2 - 3x + 9}{2x^2 + 3x + 4}$$

$$y = \frac{1}{2x^2 + 3x + 4}$$

$$y(2x^2 + 3x + 4) = 2x^2 - 3x + 9$$

$$(y-1)2x^2 + 3x(y+1) + 4y - 9 = 0$$

If 
$$y \neq 1 \Rightarrow D \geq 0$$

$$9(y + 1)^2 - 4(y - 1)(4y - 9) \ge 0$$

$$9(y^2 + 2y + 1) - 4(4y^2 - 9y - 4y + 9) \ge 0$$

$$9y^2 - 16y^2 + 18y + 52y + 9 - 36 \ge 0$$

$$-7y^2 + 70y - 27 \ge 0$$

$$7y^2 - 70y + 27 \le 0 \qquad \text{has roots } \alpha \text{ and } \beta \qquad y = \frac{70 \pm \sqrt{4900 - 4 \times 7 \times 27}}{2 \times 7}$$

$$\Rightarrow \alpha \le y \le \beta$$

$$y = \frac{70 \pm \sqrt{4144}}{14}$$

$$\alpha = m = \frac{70 - \sqrt{4144}}{14}$$

$$\beta = n = \frac{70 + \sqrt{4144}}{14}$$

$$= m + n = 10$$

13. 
$$f(x) = \begin{cases} \frac{1 - \cos 2x}{x^2} & x < 0 \\ \alpha & x = 0 \end{cases}$$
 If  $f(x)$  is continuous at  $x = 0$  find  $\alpha^2 + \beta^2$ . 
$$\beta \frac{\sqrt{1 - \cos x}}{x} \quad x > 0$$

(12)Ans.

**Sol.** 
$$\lim_{x\to 0^-} \frac{1-\cos 2x}{x^2} = 2 = \alpha = \lim_{x\to 0^+} \beta \sqrt{\frac{1-\cos x}{x^2}} = \frac{\beta}{\sqrt{2}}$$
.

Hence  $\alpha^2 + \beta^2 = 4 + 8 = 12$ 

Let  $\alpha$  and  $\beta$  be the sum and the product of all the nonzero solutions of the equation 14.  $(\overline{z})^2 + |z| = 0$ ,  $z \in C$  then  $4(\alpha^2 + \beta^2)$  is equal to

(4) Ans.

**Sol.** 
$$\bar{z}^2 + |z| = 0$$

$$x^2 - y^2 - 2xyi + \sqrt{x^2 + y^2} = 0$$

$$x = 0$$

$$y^2 = \sqrt{y^2}$$

$$y^2 = |y|$$

$$y = 1, -1$$

$$x^2 + \sqrt{x^2 + y^2} = 0$$
 No non zero solution

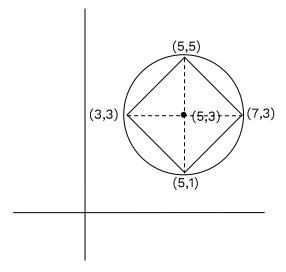
$$\alpha = 0$$

$$\beta = 1$$

$$4(\alpha^2 + \beta^2) = 4$$

A square is inscribed in the circle  $x^2 + y^2 - 10x - 6y + 30 = 0$ . One side of this square is 15. parallel to y = x + 3. If  $(x_i, y_i)$  are the vertices of the square, then  $\sum (x_i^2 + y_i^2)$  is equal to:

(3)Ans.



Sol.

$$\sum_{i} x_i^2 + y_i^2 = 25 + 25 + 49 + 9 + 25 + 1 + 9 + 9 = 152$$

If differential equation satisfies  $\frac{dy}{dx} - y = \cos x$  at x = 0,  $y = \frac{-1}{2}$ . Find  $y(\frac{\pi}{4})$ . 16.

Ans. (0)

**Sol.** 
$$\frac{dy}{dx} - y = \cos x$$

$$\mathbf{I} \cdot \mathbf{f} = \mathbf{e}^{\int -1 dx} = \mathbf{e}^{-x}$$

$$y \cdot e^{-x} = \int e^{-x} \cdot \cos x dx$$

$$I = \int e^{-x} \cos x dx$$

$$I = (-e^{-x})\cos x - \int (-\sin x)(-e^{-x})dx$$

$$I = -e^{-x} \cos x - \int e^{-x} \sin x dx$$

$$I = -e^{-x}\cos x - \left[\left(-e^{-x}\right)\sin x + \int e^{-x}\cos x dx\right]$$

$$I = -e^{-x} \cos x + e^{-x} \sin x - I$$

$$2I = e^{-x}(\sin x - \cos x)$$

$$y \cdot e^{-x} = \frac{e^{-x}(\sin x - \cos x)}{2} + c$$

$$y = \frac{(\sin x - \cos x)}{2} + c$$

$$c = 0$$

$$y\left(\frac{\pi}{4}\right) = \frac{\frac{1}{\sqrt{2}} - \frac{1}{\sqrt{2}}}{2} = 0$$

17. Let  $\alpha$ ,  $\beta$ ,  $\in$  R. Let the mean and the variance of 6 observations -3, 4, 7, - 6,  $\alpha$ ,  $\beta$  be 2 and 23 respectively. The mean deviation about the mean of these 6 observations is

(1) 
$$\frac{11}{3}$$

(2) 
$$\frac{16}{3}$$

(3) 
$$\frac{13}{3}$$

$$(4) \frac{14}{3}$$

**Ans.** (3

**Sol.** 
$$\bar{x} = 2 = \frac{-3 + 4 + 7 - 6 + \alpha + \beta}{6} \Rightarrow \alpha + \beta = 10$$

$$\sigma^2 = 23 = \frac{(-3-2)^2 + (4-2)^2 + (7-2)^2 + (-6-2)^2 + (\alpha-2)^2 + (\beta-2)^2}{6}$$

$$\Rightarrow \alpha^2 + \beta^2 = 52$$

$$\alpha = 6 \& \beta = 4$$

$$\therefore$$
 M. D. about mean =  $\frac{13}{3}$ 

**18.**  $\vec{a} = 2\hat{i} + 2\hat{j} - \hat{k}$  and  $\vec{b} = \hat{i} - \hat{k}$ ,  $\vec{c}$  is an unit vector making angle 60° with  $\vec{a}$  and 45° with  $\vec{b}$ . Find  $\vec{c}$ 

**Ans.** (1)

**Sol.** Let 
$$\vec{c} = C_1 \hat{i} + C_2 \hat{j} + C_3 \hat{k}$$
, where  $2C_1 + 2C_2 - C_3 = \frac{3}{2}$ 

$$C_1 - C_2 = 1$$

$$C_1^2 + C_2^2 + C_3^2 = 1$$
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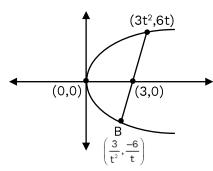
- 19. If the length of focal chord of  $y^2 = 12x$  is 15 and if the distance of the focal chord from origin is p then  $10p^2$  is equal to
  - (1) 36

(3)

- (2)25
- (3)72
- (4) 144

Ans.

Sol.



$$y^2 = 4(3)x$$
; a = 3

$$\Rightarrow$$
 focus = (3,0)

$$t_1t_2 = -1$$

$$A = 3t^2, 6t$$

then 
$$B = \frac{3}{t^2}, \frac{-6}{t}$$

AB = length of focal chord

$$= a(t_1 - t_2)^2$$

$$= 3\left(t + \frac{1}{t}\right)^2 = 15$$

$$3\left(t+\frac{1}{t}\right)^2=15$$

$$t + \frac{1}{t} = \sqrt{5}$$

$$t - \frac{1}{t} = \sqrt{\left(t + \frac{1}{t}\right)^2 - 4}$$

$$t - \frac{1}{t} = 1$$

$$m_{AB} = \frac{6t - \frac{6}{t}}{3t^2 - \frac{3}{t^2}}$$

$$m_{AB} = \frac{2}{t - \frac{1}{t}}$$

$$\therefore$$
 m<sub>AB</sub> = 2

Equation of AB: 
$$y - 0 = 2(x-3)$$

$$y = 2x - 6$$

$$2x-y - 6 = 0$$

Distance from origin, 
$$P = \frac{|2(0) - 0 - 6|}{\sqrt{2^2 + 1}} = \frac{6}{\sqrt{5}}$$

$$10P^2 = \frac{10 \times 36}{5} = 72$$

Shortest distance between lines 
$$\frac{x+1}{-2} = \frac{y}{2} = \frac{z-1}{1}$$
 and  $\frac{x-5}{2} = \frac{y-2}{-3} = \frac{z-1}{1}$  is  $\frac{38k}{6\sqrt{5}}$ , find  $\int_{-2}^{k} \left[x^2\right] dx$ 

**Ans.** 
$$(5-\sqrt{2}-\sqrt{3})$$

**Sol.** 
$$S.D = \frac{(6\hat{i} + 2\hat{j}).(5\hat{i} + 4\hat{j} + 2\hat{k})}{\sqrt{45}} = \frac{38}{3\sqrt{5}} = \frac{38k}{6\sqrt{5}} \Rightarrow k = 2$$

$$\int_{0}^{2} [x^{2}] dx = \int_{1}^{\sqrt{2}} dx + \int_{1/2}^{\sqrt{3}} 2dx + \int_{1/2}^{2} 3dx = (\sqrt{2} - 1) + 2(\sqrt{3} - \sqrt{2}) + 3(2 - \sqrt{3}) = 5 - \sqrt{2} - \sqrt{3}$$

21. 
$$y = y(x)$$
 is a solution of the differential equation 
$$\left(x^4 + 2x^3 + 3x^2 + 2x + 2\right) dy - \left(2x^2 + 2x + 3\right) dx = 0. \text{ If } y\left(0\right) = \frac{\pi}{4}. \text{ Find } y(-1)$$

Ans. 
$$\left(-\frac{\pi}{4}\right)$$

Sol. 
$$\frac{dy}{dx} = \frac{2x^2 + 2x + 3}{x^4 + 2x^3 + 3x^2 + 2x + 2}$$
$$\frac{dy}{dx} = \frac{(x^2 + 1) + (x^2 + 2x + 2)}{(x^2 + 1)(x^2 + 2x + 2)} = \frac{1}{(x + 1)^2 + 1} + \frac{1}{x^2 + 1}$$

Hence 
$$y = tan^{-1}x + tan^{-1}(x+1) + c$$

If 
$$y(0) = \frac{\pi}{4} \Rightarrow c = 0$$

So 
$$y(-1) = -\frac{\pi}{4}$$

Curve y = 1 + 3x - 2x² and y = 
$$\frac{1}{x}$$
 intersects at point  $\left(\frac{1}{2},2\right)$  then area enclosed between curve is  $\frac{1}{24}\left(\ell\sqrt{5}+m\right)-n\log_{e}\left(1+\sqrt{5}\right)$  then find the value of  $\ell+m+n$  is

**Sol.** 
$$1+3x-2x^{2} = \frac{1}{x}$$

$$\Rightarrow x+3x^{2}-2x^{3} = 1$$

$$\Rightarrow 2x^{3}-3x^{2}-x+1=0$$

$$\Rightarrow 2x^{3}-x^{2}-2x^{2}+x-2x+1=0$$

$$\Rightarrow (2x-1)x^{2}-x(2x-1)-1(2x-1)=0$$

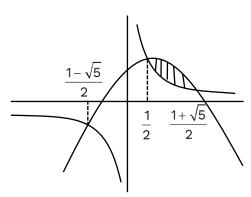
$$\Rightarrow (2x-1)\left(x^{2}-x-1\right)=0$$

$$x = \frac{1}{2} \quad \text{or} \quad x^{2}-x-1=0$$

$$x = \frac{1\pm\sqrt{5}}{2}$$

$$\begin{split} x &= \frac{1+\sqrt{5}}{2}, \frac{1-\sqrt{5}}{2} \\ \text{Area} &= \int_{1/2}^{\frac{\sqrt{5}+1}{2}} \left( \left( -2x^2 + 3x + 1 \right) - \frac{1}{x} \right) \mathrm{d}x \\ &= \left[ -\frac{2x^3}{3} + \frac{3x^2}{2} + x - \ln x \right]_{1/2}^{\frac{\sqrt{5}+1}{2}} \\ &= \left( -\frac{2}{3} \left( \frac{\sqrt{5}+1}{2} \right)^3 + \frac{3}{2} \left( \frac{\sqrt{5}+1}{2} \right)^2 + \left( \frac{\sqrt{5}+1}{2} \right) - \ln \left( \frac{\sqrt{5}+1}{2} \right) \right) \\ &- \left( -\frac{1}{12} + \frac{3}{8} + \frac{1}{2} - \ln \frac{1}{2} \right) \\ &= -\frac{1}{12} (5\sqrt{5} + 1 + 3\sqrt{5} (\sqrt{5} + 1)) + \frac{3}{8} (6 + 2\sqrt{5}) + \frac{\sqrt{5}+1}{2} \\ &- \ln(\sqrt{5} + 1) + \ln 2 - \left( \frac{-2+9+12}{24} \right) - \ln 2 \\ &= -\frac{1}{12} (16 + 8\sqrt{5}) + \frac{3}{4} (3 + \sqrt{5}) + \frac{\sqrt{5}+1}{2} - \frac{19}{24} - \ln(\sqrt{5}+1) \\ &= \frac{1}{24} [-32 - 16\sqrt{5} + 54 + 18\sqrt{5} + 12\sqrt{5} + 12 - 19] - \ln(\sqrt{5}+1) \\ &= \frac{1}{24} [15 + 14\sqrt{5}] - \ln(\sqrt{5}+1) \\ &\text{So} \quad \ell = 14, \ m = 15, \ n = 1 \end{split}$$

Hence  $\ell$  + m + n = 14 + 15 + 1 = 30



#### **PHYSICS**

**1.** A metallic wire of uniform mass density having mass M and length l is bent to form a semicircle. A point mass m is kept at the centre of the semicircle. Find the gravitational forced experienced by m.

Ans. 
$$\frac{2\pi GMm}{L^2}$$

**Sol.** 
$$r = \frac{L}{\pi}$$

$$dg = \frac{Gdm}{r^2} \sin \theta$$

$$G M$$

$$= \frac{G}{r^2} \frac{M}{L} r d\theta \sin \theta$$

$$= \frac{G}{g} = \frac{G}{r} \cdot \frac{M}{L} \int_{0}^{\pi} \sin \theta d\theta$$

$$g = \frac{GM}{rL}(2)$$

$$= m^2 \frac{GM}{rL}$$

$$= \frac{2GMm}{L} \frac{\pi}{L}$$

$$= \frac{2\pi GMm}{L^2}$$

9 Sin 9 Sin 9 M

- 2. 5 convex lens are kept together each having power of 25 D. Find the focal length.
- **Ans.** 0.8 cm

**Sol.** 
$$P_{eq} = P \times 5$$

$$\frac{1}{f_{eq}} = 125 \text{ m}$$

$$=\frac{100}{125}$$
 cm

$$=\frac{4}{5}$$
 cm

$$= 0.8 cm$$

- **3.** Position of a particle is related to time as given equation  $x = t^4 + 6t^2 + 2t$ 
  - Find its acceleration at t = 5 sec.

**Sol.** 
$$V = \frac{dx}{dt}$$

$$V = 4t^3 + 18t^2 + 2$$

$$a=\frac{dV}{dt}$$

$$= 12t^2 + 36 t$$

At 
$$t = 5 sec$$

$$a = 12 \times 25 + 36 \times 5$$

$$= 300 + 180$$

$$= 480 \text{ m/s}^2$$

4. A body moving with constant acceleration covers 102.5 m in nth second of its motion and covers 115.0 m in (n + 2)<sup>th</sup> second then find its acceleration.

6.25 m/s<sup>2</sup> Ans.

Let, acceleration = a (constant) Sol.

$$S_{n^{th}} = u + \frac{a}{2}[2n - 1] = 102.5$$
 ...(i)

$$S_{(n+2)^{th}} = u + \frac{a}{2}[2(n+2) - 1] = 115$$

$$\Rightarrow$$
 u +  $\frac{a}{2}$ [2n + 3] = 115 ...(ii)

by using (i) and (ii)

$$102.5 - \frac{a}{2}[2n - 1] + \frac{a}{2}[2n + 3] = 115$$

$$\Rightarrow$$
 102.5 +  $\frac{a}{2}$  +  $\frac{3a}{2}$  = 115

$$\Rightarrow$$
 2a = 115 - 102.5

$$a = \frac{12.5}{2} = 6.25 \text{m} / \text{s}^2$$

- 5. A particles of mass m dropped from height h above the ground. After collision, rises to height h/2, Then loss in energy during collision and speed of particle just before collision respectively are.
  - (1) 50%,  $\sqrt{2gh}$
- (2) 40%,  $\sqrt{2gh}$  (3) 50%,  $\sqrt{gh}$  (4) 40%,  $\sqrt{gh}$

Ans.

- $\Delta E = mg \frac{h}{2} mgh = -mg \frac{h}{2}$ Sol.
  - i.e. 50% loss in energy

$$v = \sqrt{2gh}$$

If the electric field vector at a point in an electromagnetic wave is given by 6.  $\vec{E} = 40\cos\omega\left(t - \frac{z}{c}\right)\hat{i}$  then corresponding  $\vec{B}$  will be:

**Sol.** 
$$\vec{E} = 40 \cos \omega \left( t - \frac{z}{c} \right) \hat{i}$$

$$|\vec{E}| = 40 \cos \omega \left(t - \frac{z}{c}\right)$$

$$\frac{|\vec{E}|}{|\vec{B}|} = C$$

$$|\vec{B}| = \frac{40}{C} \cos \omega \left( t - \frac{z}{C} \right); \text{ also } \vec{E}.\vec{B} = 0$$

**7.** Infinite charge sheet in xy plane of surface charge density  $\sigma$  and infinite long wire of linear charge density  $\lambda$  placed at (0, 0, 4) and  $\sigma = 2\lambda$ . Then net electric field (0, 0, 2).

Ans. 
$$E_{net} \Rightarrow \frac{\lambda}{\epsilon_0} \left[ \frac{2\pi r - 1}{2\pi r} \right] N/C$$

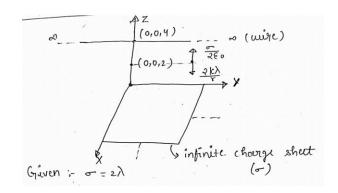
Sol. Given :  $\sigma = 2\lambda$ 

$$E_{net} = \frac{\sigma}{2\epsilon_0} - \frac{2K\lambda}{r}$$

$$E_{net}\!=\!\frac{2\lambda}{2\epsilon_0}\!-\!\frac{2\lambda}{4\pi\epsilon_0 r}$$

$$E_{net} = = \frac{2\lambda}{2\epsilon_0} - \frac{2\lambda}{4\pi\epsilon_0 r}$$

$$\Rightarrow \frac{\lambda}{\epsilon_0} \left[ \frac{2\pi r - 1}{2\pi r} \right] N/C$$



**8.** A hollow cylinder and solid sphere of same mass and radius are rolling with same initial velocity v on a rough inclined plane. Find the ratios of their kinetic energies and maximum height reached by them.

**Ans.** 
$$\frac{10}{7}$$

**Sol.** 
$$K_{cylinder} = \frac{1}{2}MV^2 + \frac{1}{2}I_{cm}\omega^2 = \frac{1}{2}MV^2 + \frac{1}{2}(MR^2)\left(\frac{V}{R}\right)^2$$

$$K_{\text{sphere}} = \frac{1}{2}I_{\text{cm}}\omega^2 + \frac{1}{2}MV^2$$

$$=\frac{1}{2}\left(\frac{2}{5}MR^{2}\right)\left(\frac{V}{R}\right)^{2}+\frac{1}{2}MV^{2}$$

$$=\frac{1}{5}MV^2 + \frac{1}{2}MV^2$$

$$= \frac{7}{10}MV^2$$

$$\Rightarrow \frac{\mathsf{K}_{\mathsf{cylinder}}}{\mathsf{k}_{\mathsf{sphere}}} = \frac{10}{7}$$

At top point kinetic energy will convert into potential energy

$$\frac{\text{Mgh}_{\text{cylinder}}}{\text{Mgh}_{\text{sphere}}} = \frac{10}{7}$$

$$\Rightarrow \frac{h_{cylinder}}{h_{sphere}} = \frac{10}{7}$$

9. In given equation  $y = 2A \sin\left(\frac{2\pi nt}{\lambda}\right) \cos\left(\frac{2\pi x}{\lambda}\right)$ . Find the dimension of n.

**Ans.** 
$$[n] = [L^1T^{-1}]$$

**Sol.** 
$$[n] \Rightarrow \frac{[2\pi nt]}{[\lambda]} + M^0L^0T^0$$

$$\frac{[n][T^1]}{[L^1]} = M^0L^0T^0$$

$$[n] = [L^1T^{-1}]$$

- 10. When a conducting platinum wire is placed in ice, its resistance is  $8\Omega$  and when placed in steam it is  $10\Omega$ . Find the resistance of wire at  $400^{\circ}$ C.
- Ans.  $8.8\Omega$
- **Sol.**  $R_T = R_0 (1 + \alpha \Delta T)$

$$R_0$$
 at 0°  $\Rightarrow$  8 $\Omega$ 

$$R_T$$
 at 100°C  $ightarrow$  10 $\Omega$ 

$$10 = 8(1 + \alpha(100))$$

$$\frac{10}{8} = 1 + 100\alpha$$

$$\left(\frac{10}{8} - 1\right) \times \frac{1}{100} = \alpha$$

$$\alpha = \frac{2}{8} \times \frac{1}{100}$$

$$\alpha = \frac{1}{400}$$

$$R = R_0(1 + \alpha \Delta T)$$

$$=8\left(1+\frac{1}{400}\times40\right)$$

$$= 8 \left(1 + \frac{1}{10}\right)$$

$$=\frac{11\times8}{10}$$

$$R = 8.8\Omega$$

11. Fractional error in image distance and object distance are  $\frac{\Delta v}{v}$  and  $\frac{\Delta u}{u}$  then find the fractional error in focal length of the given spherical mirror.

Ans. 
$$\Rightarrow \frac{df}{f} = \frac{uv}{u+v} \left[ \frac{dv}{v^2} + \frac{du}{u^2} \right]$$

$$Sol. \qquad \frac{1}{f} = \frac{1}{v} + \frac{1}{u}$$

$$\frac{1}{f} = \frac{u + v}{uv}$$

$$f = \frac{uv}{u+v}$$

$$\Rightarrow -\frac{1}{f^2}df = -\frac{dv}{v^2} - \frac{du}{u^2}$$

$$\Rightarrow \frac{df}{f} = f \left[ \frac{1}{v} \frac{dv}{v} + \frac{1}{u} \frac{du}{u} \right]$$

$$\Rightarrow \frac{df}{f} = \frac{uv}{u+v} \left[ \frac{dv}{v^2} + \frac{du}{u^2} \right]$$

- 12. Instantaneous current in a circuit is zero. In which of the options voltage will be maximum.
  - (a) L
- (b) C
- (c) R
- (d) LC

- (1) ABD
- (2) B
- (3) BC
- (4) D

- (1)
- **Sol.** Phase difference between current and voltage is 90°.

So, possible circuit are (A), (B) and (D).

13.

x and y coordinates of a body performing some motion is given as:

$$x = 3 + 4t$$

$$y = 3t^2 + 4t$$

Identify the trajectory of motion.

- (1) Parabola
- (2) Circular
- (3) Straight line
- (4) Hyperbola

Ans.

$$x = 3 + 4t \implies t = \frac{x - 3}{4}$$

$$y = 3t^2 + 4t$$

equation (1) in (2)

$$y = 3 \frac{(x-3)^2}{16} + 4 \frac{(x-3)}{4}$$

$$\Rightarrow$$
 y =  $\frac{3}{16}$ (x<sup>2</sup> + 9 - 6x) + (x - 3)

$$\Rightarrow y = \frac{1}{16} \left[ 3x^2 + 27 - 18x + 16x - 48 \right]$$

$$y = \frac{1}{16} \left[ 3x^2 - 2x - 21 \right]$$

- $\Rightarrow$  it is quadratic in x
- $\Rightarrow$  its trajectory is parabola.

14.

Choose the correct graph for kinetic energy vs r for an electron revolving around a infinite line of charge.

- Ans.
- Theoretical

Sol.

. Net force acting towards centre =  $\frac{mv^2}{r}$ 

$$F = q \times E$$

$$F = e \times 2k \frac{\lambda}{r}$$

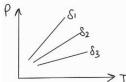
$$\Rightarrow \frac{mv^2}{r} = (e)\left(\frac{2k\lambda}{r}\right)$$

$$mv^2 = 2k\lambda \times e$$

$$\Rightarrow$$
 KE =  $2k\lambda e$ 

KE 2kλe

**15.** Pressure vs temperature graph is given for gas of different density. Compare  $\rho_1$ ,  $\rho_2$  and  $\rho_3$ ?





$$\rho_1 > \rho_2 > \rho_3$$

Sol.

$$PM = \rho RT$$

$$\rho = \frac{1}{RT}$$

$$\rho \propto \frac{P}{T}$$

Hence  $\rho_1 > \rho_2 > \rho_3$ 

- **16.** Work done to expand the bubble of diameter 7 cm and surface tension 40 dyne/cm is 36960 erg. Find the radius of the expanded bubble?
- **Ans.** 14 cm
- **Sol.** Surface energy = T (area)
  - Bubble has tw surface of interface
  - $E_i = 2TS_i$
  - $E_f = 2TS_f$
  - $\Rightarrow$  Work done =  $E_f E_i$
  - $\Rightarrow$  36960 = 2[TS<sub>f</sub> -TS<sub>i</sub>]
  - ⇒ 3690 = TΔS ×2
  - $\Rightarrow \Delta S = \frac{36960}{40 \times 2}$
  - $\Rightarrow \Delta S = 462 \text{ cm}^2$
  - $S_f S_i = 462$
  - $\Rightarrow 4\pi r_f^2 = 462 + 4\pi r_i^2$
  - $\Rightarrow r_f^2 = \frac{1}{4\pi} \left\lceil 462 + 4\pi \times \left(\frac{7}{2}\right)^2 \right\rceil$
  - $r_f^2 = \frac{1}{4\pi} [462 + 4\pi \times \frac{49}{4}]$
  - $= \frac{462 \times 7}{4 \times 22} + \frac{49}{4}$
  - $= r_f^2 = \frac{196}{4} = 49$
  - $r_f = 7 \text{ cm}$
  - diameter =  $7 \times 2 = 14$  cm
- 17. De-Broglie wavelength of electron moving from n = 4 to n = 3 of a hydrogen is  $b(\pi a)$ ; Where a is bohr radius of the hydrogen atom. Find the value of b.
- Ans. b = 2
- **Sol.**  $E = \frac{hc}{\lambda}$ ,  $mvr = \frac{nh}{2\pi}$ 
  - $\lambda = \frac{h}{mv} = \frac{2\pi r}{n}$
  - $(\lambda_1)_{n=4} = \frac{(2\pi)(a_0^2)}{n}$
  - $(\lambda_1)_{n=4} = (2\pi)(a_0 n) = 8\pi a_0$
  - $\left(\lambda_2^{}\right)_{n=3}^{}=6\pi a_0^{}$
  - $\Delta\lambda = \lambda_1 \lambda_2 = 8\pi a_0 6\pi a_0$
  - $\Delta \lambda = 2\pi a_0$
  - Therefore b = 2
- **18.** An elastic string under tension of 3N has a length of 'a'. If length is 'b' then tension is 2N. Find tension when length is (3a 2b).
- Ans.  $\frac{SF}{K}$
- **Sol.** F = kx
  - $3F = Ka \Rightarrow a = \frac{3F}{K}$
  - $2F = Kb \Rightarrow b = \frac{2F}{K}$

Now, 
$$3a-2b = \frac{9F}{K} - \frac{4F}{K} = \frac{5F}{K}$$

**19.** An electron projected inside the solenoid along its axis which carries constant current, then its trajectory would be:

Ans. Straight line

Sol.

$$\vec{F} = q(\vec{V} \times \vec{B})$$

 $\vec{B}$  and  $\vec{V}$  are parallel at axis of solenoid so, their cross product will be zero

i.e. 
$$\vec{F} = 0$$

So, electron will move with constant velocity in a straight line.

**20.** Current as a function of time is given as  $i = 6 + \sqrt{56} \sin \left( 100t + \frac{\pi}{3} \right)$  A. Find rms value of current.

**Ans.** 8 A

**Sol.** 
$$i_{rms} = \sqrt{6^2 + \frac{(\sqrt{56})^2}{2}}$$
$$= \sqrt{36 + 28}$$

$$=\sqrt{64}$$

21. In Celsius the temperature of a body increases by 40°C. The increasing temperature on Fahrenheit scale is:

**Ans.** 72°F

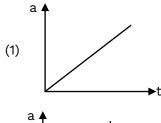
**Sol.** 
$$T_F = \frac{9}{5}T_c + 32$$

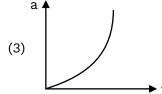
$$\Delta T_{\rm f} = \frac{9}{5} \Delta T_{\rm c}$$

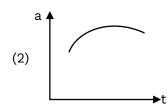
$$\Rightarrow \Delta T_F = \frac{9}{5} \times 40$$

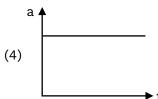
$$\Rightarrow \Delta T_F = 72^{\circ} F$$

**22.** Force on a particle varies linearly with time(t) (F  $\propto$  t). Then select correct acceleration vs time graph.







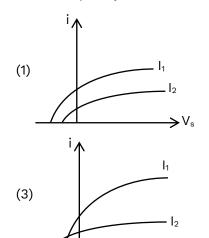


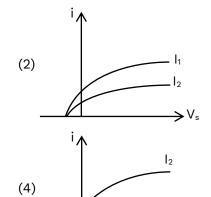
**Ans.**  $\Rightarrow$  a  $\propto$  t

**Sol.** 
$$F = ma \Rightarrow a = \frac{F}{m}$$

$$\Rightarrow$$
 a  $\propto$  t

Which graph correctly represents the photo current (i) vs stopping potential  $(V_s)$  for the same frequency but different intensity? (Here  $I_1 > I_2$ )

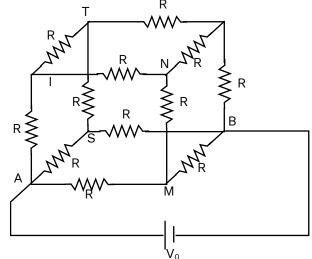




Ans.

Theoretical

**24.** A cubical arrangement of 12 resistors each having resistance R is shown. Find I shown in the given circuit.



Ans. 
$$\frac{V}{6}$$

**Sol.** 
$$\frac{1}{R_{eq}} = \frac{1}{3R} + \frac{1}{R} = \frac{4}{3R}$$

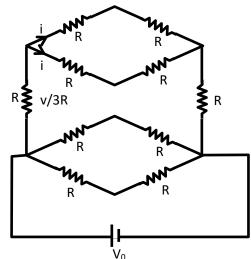
$$R_{eq} = \frac{3R}{4}$$

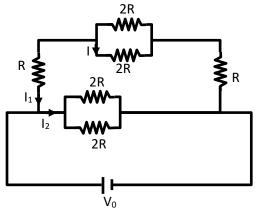
$$\Rightarrow V_0 = IR_{eq}$$

$$\Rightarrow I = \frac{4V_0}{3R}$$

So. 
$$l_1 + l_2 = l$$

 $\Rightarrow\!$  in parallel combination, current is divided into inverse ratio of resistance

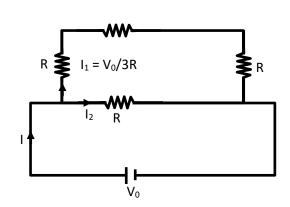




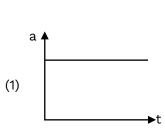
$$\Rightarrow \frac{l_1}{l_2} = \frac{l}{3}$$

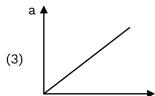
$$\Rightarrow \ I_1+3I_1=I\Rightarrow I_1=\frac{1}{4}I=\frac{V_0}{3R}$$
 Now,  $I_1$  gets divided equally in both branches

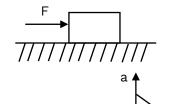
$$i = \frac{l_1}{2} = \frac{V_0}{3R} \times \frac{1}{2} \implies i = \frac{V_0}{6R}$$

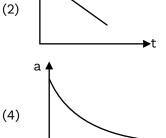


25. A wooden block is initially at rest on at rest a smooth surface. Now a horizontal force is applied on the block which increases linearly with time. The acceleration time (a-t) graph for the block would be:









Ans. 
$$F = \frac{k}{m}t$$

This horizontal force increases linearly with time

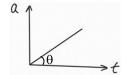
$$F \propto t$$

$$F = kt + c$$

$$a = \frac{k}{m}t + \frac{c}{m}$$

if, 
$$\frac{c}{m} = 0$$

$$\tan\theta = \frac{k}{m}$$

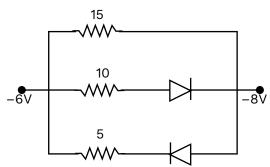


then:

$$\Rightarrow$$
 F = kt

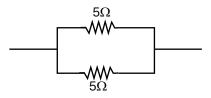
$$\Rightarrow$$
 a = F =  $\frac{k}{m}$  t

# **26.** Find R<sub>eq</sub> ?



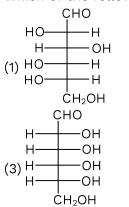
**Sol.** Below diode is in reverse bias so no current flow through it circuit looks like.

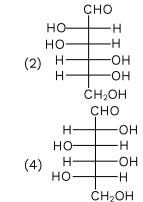
$$R_{e\,q}=\frac{5}{2}=2.5\Omega$$



## **CHEMISTRY**

1. Which of the following is the correct structure of L-Glucose





**Ans.** (1)

- **Sol.** Structure based
- **2.** How many structural isomer are there in  $C_7H_{16}$ 
  - (1) 5
- (2) 6
- (3) 8
- (4)9

**Ans.** (4)

- **Sol.** 9 structural isomers are possible of  $C_7H_{16}$
- **3.** Which of the following has the maximum dipole moment
  - (1) NH<sub>3</sub>
- (2) NF<sub>3</sub>
- (3) PCl<sub>5</sub>
- $(4) CH_4$

**Ans.** (1)

- **Sol.** NH<sub>3</sub> has maximum dipole moment
- **4.** Which of the following show only one oxidation state except it's elemental state
  - (1) Ti
- (2) Sc
- (3) Co
- (4) Ni

**Ans.** (2)

- **Sol.** Sc show only +3 oxidation state.
- **5.** Number of species having sp<sup>3</sup> hybridised central atom
  - $NO_3^-$
- $BCl_3$
- ClO<sub>2</sub>-
- ClO<sub>3</sub>-

**Ans.** (02.00)

- **Sol.** Cl atom in ClO<sub>2</sub><sup>-</sup> and ClO<sub>3</sub><sup>-</sup> molecule is sp<sup>3</sup> hybridised.
- **6.** Number of complexes having even number of unpaired electron in d-orbital.

 $[\text{Cu}(\text{H}_2\text{O})_6]^{2+}$  ,  $[\text{Fe}(\text{H}_2\text{O})_6]^{3+}$  ,  $[\text{Cr}(\text{H}_2\text{O})_6]^{2+}$  ,  $[\text{Ni}(\text{H}_2\text{O})_6]^{2+}$ 

**Ans.** (02.00)

**Sol.** All are octahedral complex

| Complex             | Number of unpaired electron |
|---------------------|-----------------------------|
| $[Cu(H_2O)_6]^{2+}$ | 1                           |
| $[Fe(H_2O)_6]^{3+}$ | 5                           |
| $[Cr(H_2O)_6]^{2+}$ | 4                           |

$$[Ni(H_2O)_6]^{2+}$$

7. If emf of hydrogen electrode at 25°C is zero pure water then pressure of  $H_2$  in bar

$$(2)\ 10^{-7}$$

(1) Ans.

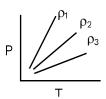
**Sol.** 
$$H^+ + e^- \longrightarrow \frac{1}{2} H_2$$

$$\varepsilon = 0 - \frac{0.059}{1} log \frac{\left(P_{H_2}\right)^{1/2}}{10^{-7}}$$

$$\frac{\left(P_{H_2}\right)^{1/2}}{10^{-7}} = 1$$

$$P_{H_2} = 10^{-14}$$

8. Pressure v/s temperature graph of an ideal gas of equal number of moles of different density is given below:



$$\rho_1 = \rho_2 = \rho_3$$

(2) 
$$\rho_1 > \rho_2 > \rho_3$$

T
(1) 
$$\rho_1 = \rho_2 = \rho_3$$
(2)  $\rho_1 > \rho_2 > \rho_3$ 
(3)  $\rho_1 < \rho_2 < \rho_3$ 
(4)  $\rho_1 > \rho_2 < \rho_3$ 

(4) 
$$\rho_1 > \rho_2 < \rho_3$$

Ans.

**Sol.** 
$$P = \frac{R\rho}{M}T$$

Slope = 
$$\frac{R\rho}{M} \propto \rho$$

$$\rho_1 > \rho_2 > \rho_3$$

Total number of species having single unpaired electron in NO,  $\bar{\rm C}{\rm N}$  ,  ${\rm O}_2^{\rm -}, {\rm O}_2^{\rm 2-}, {\rm O}_2$ 9.

(02.00)Ans.

**Sol.** NO total 
$$e^- = 15$$

NO total 
$$e^- = 15$$
 Unpaired  $e^- = 1$ 

$$CN^-$$
 total  $e^- = 14$  Unpaired  $e^- = 0$ 

$$O_2^-$$
 total  $e^- = 17$  Unpaired  $e^- = 1$ 

$$O_2^{2-}$$
 total  $e^- = 18$  Unpaired  $e^- = 0$ 
 $O_2$  total  $e^- = 16$  Unpaired  $e^- = 2$ 

(1) Be 
$$<$$
 B  $<$  O  $<$  F  $<$  N

Ans. (2)

**Sol.** Be 
$$>$$
 B  $<$  N  $>$  O  $<$  F

$$2s^2$$
  $2p^1$   $2p^3$   $2p^4$   $2p^5 \rightarrow$  electronic configuration

Correct order

B< Be < O < N < F

11. For any reaction 
$$K = \frac{K_1 K_2}{K_3}$$
 and  $Ea_1 = 400, Ea_2 = 300, Ea_3 = 200$  hence  $E_{overall}$ ?

- (1) 400
- (2) 200
- (3) 500
- (4)600

**Ans.** (3)

**Sol.** 
$$E_{overall} = Ea_1 + Ea_2 - Ea_3$$
  
=  $400 + 300 - 200 = 500$ 

12. If weight of NaCl in 500ml aqueous solution is 5.85 gm hence calculate the molarity?

**Ans.** (00.20)

**Sol.** 
$$\left[NH_3\right] = \frac{n}{v} = \frac{5.85 / 58.5}{0.5} = 0.2M$$

2M, 2ml solution of KMnO<sub>4</sub> is neutralised with 20 ml H<sub>2</sub>C<sub>2</sub>O<sub>4</sub>. Calculate molarity of H<sub>2</sub>C<sub>2</sub>O<sub>4</sub>

**Ans.** (00.50)

**Sol.** 
$$MnO_4^-$$
 +  $C_2O_4^{2-}$   $\xrightarrow{H^+}$   $Mn^{2+}$  +  $CO_2$ 

$$n_f = 5$$
  $n_f = 2$ 

$$2 \times 5 \times 2 = M \times 2 \times 20$$

$$M = 0.5 M$$

**14.** De-Broglie wavelength of  $e^-$  4<sup>th</sup> orbit of H-Atom is  $x\pi r_0$ , where  $r_0$  = bohr's I<sup>st</sup> orbit radius of H-Atom x is\_\_\_\_

**Ans.** (8)

**Sol.** 
$$4\lambda = 2\pi r_A$$

$$\lambda = \frac{2\pi}{4} r_0 \times 4^2$$

$$=8\pi r_0$$

**15.** Among which of the following decreasing order of basic strength will be

- (i) OH-
- (ii) H<sup>-</sup>
- (iii) HCOO-
- (iv) CH<sub>3</sub>COO-

- (v) —OR
- (1) || > V > || > | > |V

(2) |I| > V > I > |V| > |I|

(3) | || > V| > | > V > ||

**Ans.** (2)

**Sol.** The order of basic strength is as follows:

$$H^- > -OR > OH^- > CH_3COO^- > HCOO^-$$

**16.** What type of electrode is calomel?

(1) redox electrode

(2) metal-metal insoluble salt-its anion

(3) gas-ion

(4) metal-metal ion

**Ans.** (2)

**Sol.** metal-metal insoluble salt-its anion.

- 17. Total number of elements which do not use all valence electrons in bonding as per their group number among them O, S, F, N, Al, C, Si
- (03.00)Ans.

Si

- Sol. Valance Electron 6 0 S 6 F 7 N 5 Αl 3 С
- Identify the suitable reagents X and Y for given below reaction respectively 18.

$$\begin{array}{c|c} & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\$$

- (1) dil. NaOH/20°; HBr/CH<sub>3</sub>-COOH
- (2) dil. NaOH/20°; Br<sub>2</sub>/CH<sub>3</sub>-COOH
- (3) Alcoholic NaOH/80°; HBr/CH₃COOH
- (4) Alcoholic NaOH/80°; HBr/Peroxide

(3)Ans.

19.

- Compare ligand strength of F-, OH-, SCN-, CO
  - (1)  $CO > OH^- > F^- > SCN^-$

(2)  $CO > F^- > OH^- > SCN^-$ 

(3)  $SCN^{-} > OH^{-} > F^{-} > CO$ 

 $(4) F^{-} > CO > OH^{-} > SCN^{-}$ 

- Ans.
- SFL (Strong Field Ligand) > WFL (Weak Field Ligand) Sol.
  - C/N/P

- O/Halogens/S
- 20. Which of the following compound will not give the test of nitrogen by the help of lassaigne's extract?
  - (1) Hydrazine

(2) Phenyl hydrazine

(3) Glycine

(4) Urea

- Ans. (1)
- Sol. Hydrazine (NH<sub>2</sub>NH<sub>2</sub>) does not contain carbon On fusion with Na metal, it cannot cannot form NaCN. So hydrazine does not show lassaigne's test.

21.  $K_2MnO_4 \xrightarrow{\text{alkaline}} KMnO_4 + MnO_2$ 

Find the sum of spin only magnetic moment of central metal ion in both the products. (nearest integer)

**Ans.** (04.00)

**Sol.**  $KMnO_A \rightarrow Mn \Rightarrow d^0 \quad \mu = 0$ 

$$MnO_2 \rightarrow Mn \Rightarrow 3d^3 \quad \mu = 3.87$$

nearest integer = 4

22. During the test of group IV NH<sub>4</sub>Cl is added with NH<sub>4</sub>OH why?

- (1) to increase the concentration of OH- ion
- (2) to decrease the concentration of OH- ion
- (3) to increase the concentration of H+ ion
- (4) to decrease the concentration of H<sup>+</sup> ion

**Ans.** (2

**Sol.** NH<sub>4</sub>Cl is added with NH<sub>4</sub>OH to decrease the concentration of OH<sup>-</sup> ion in order to avoid precipitation of further group elements.

23. Statement-I:  $\alpha$ -H is responsible for carbonyls giving aldol

Statement-II: Benzaldehyde & ethanal show cross aldol

- (1) Both statements are correct
- (2) statements-I is correct and statement-II is incorrect
- (3) statements-II is correct and statement-I is incorrect
- (4) Both statements are incorrect

**Ans.** (1)

**Sol.** Statement-I: Aldol condensation is proceed through  $\alpha$ -hydrogen  $\Rightarrow$  True

**Statement-II:** Ethanal have  $\alpha$ -hydrogen hence it shows cross aldol  $\Rightarrow$  True

**24.** What is the correct product in below given reaction

etion 
$$\xrightarrow{Zn-Hg/HCl}$$
 Product

CHO

**Ans.** (1

**Sol.** Clemmensen Reduction is used to reduce aldehyde & ketone into its respective alkane.

$$\begin{array}{c|c}
O \\
R_1
\end{array}
\xrightarrow{R_2}
\xrightarrow{Zn-Hg}
\xrightarrow{HCI}
\xrightarrow{R_1}
\xrightarrow{H}$$