NEET Revision Notes Physics Alternating Current

Direct current is the current that may or may not change in magnitude but does not change in its direction.

I□*I*Osin □*t* Or /□/ Oco§*lt* Alternating current is the current which changes continuously in magnitude and direction periodically. It can be represented by a sine curve or a cosine curve

Here, 1^0 is peak value of current and is known as amplitude of ac, 1 is instantaneous value of alternating current.

 $\square \square \mathcal{I}\mathcal{T} \square \mathcal{I}\square$ where T is the period of ac and v is frequency.

Mean or average value of alternating current or volts over one complete cycle:

● The mean or average value of alternating current voltage over one complete cycle is zero.

$$
\begin{array}{cc}\nI_{\alpha\nu}\text{ or } I & \text{or } I_{\alpha\nu} \Box \overline{U}^T \text{ is in}\Box dt_{\Box 0\text{, }V_{\gamma\gamma}\text{ or }V\text{ or }V_{\alpha n}\Box \overline{U}^T \text{ is in}\Box dt_{\Box 0} \\
& \overline{U}_{\alpha\beta}^T \text{ and } U & \overline{U}_{\alpha\beta}^T \end{array}
$$

● Average value of alternating current for first half equation is:

$$
\text{I}\text{C}\text{C}\text{C}\text{D}^{\text{L}^{3/2}}\text{I}\text{S}\text{in}\text{L}^{2I}\text{D}\text{D}^{2I}\text{C}\text{D}^{2I}\text{D
$$

\n- Similarly, for alternating voltage, the average value of first half cycle is
\n- $$
V_{\alpha} \Box \overline{d}^{1/2} V_{\beta} \Pi \Box dt \quad \Box \quad \Box \quad \Box \quad \Box \quad \Box
$$
\n
\n- $$
V_{\alpha} \Box \overline{d}^{1/2} dt \quad \Box \quad \Box
$$
\n
\n

● Average value of alternating current for second cycle is

T T I sin*dt* 2*I Ia* ⁰ *v* 0.637*I*0 /2 0 *T T* /2 *dt*

Root Mean Square (rms) Value of Alternating Current:

It is defined as that value of steady current, which would generate the same amount of heat in a given resistance in a given time, as is done by the alternating current when passed through the same resistance for the same time. The RMS value of alternating current is also known as the effective valaus prisiraplesalnuted by_{rms},leffor l_v.

$$
I_{rms} \text{ or } I \vee \Box \frac{I_0}{\sqrt{2}} \Box 0.70710
$$

Similarly, for alternating voltage:

$$
V_{rms} \text{ OR } V \text{ rms} \Box \frac{V_0}{\sqrt{2}} \Box 0.707V0
$$

Form factors:

Form factor is ratio of rms value to average value of alternating current or voltage

during half cycle. Form factor
$$
\frac{I_{rms}}{I_{av}} = \frac{\frac{I_o}{\sqrt{2}}}{\frac{2I_o}{\Box}} = \frac{\Box}{2\sqrt{2}} = 11.11
$$

AC Circuit Containing Pure Resistance only:

 \bullet Let *V*^I*V* 0sin^I*t Image: AC circuit with pure resistor*

 \bullet Then, $I\Box \veeeq I\Box$ \bullet $I\Box$ I 0sin $\Box t$ *R R*

● Here the alternating voltage is in phase with current, when ac flows through a resistor.

Image: Phasor graph of a resistive circuit

AC Circuit Containing Pure Inductor only:

Image: Phasor graph for a inductive circuit

AC Circuit Containing Pure Capacitor only:

ac flows through a capacitor.

● Capacitive reactance: It is the opposition offered by the capacitor to the flow of alternating current through it. The capacitive reactance is infinite for dc \Box \Box \Box \Box \Box \Box and has a finite value for ac.

\n
$$
\begin{array}{r}\n \chi \subset \Box \quad \Box \quad \Box \\
 \hline\n \Box \quad \Box \quad \Box \quad \Box \\
 \hline\n \end{array}
$$
\n

\n\n The capacitance reactance is infinite to find $\text{d}\Box$ and has a finite value for ac .\n

2

Image: Phasor graph of a capacitive circuit

AC circuit with an inductor and a resistor:

A circuit with an inductor and a resistor is called an LR circuit in series. Here,

 $Z \Pi/R2 \Pi/M$ \cong the impedance of the circuit.

Image: LR circuit with phasor diagram

As in the figure the current lags the voltage by an angle $\tanh^2\Box\to\Box$ *R* ngletand^{1 ∐} 日 \Box \Box \Box \Box

AC circuit with an inductor and a capacitor:

A circuit which has an inductor and capacitor connected in series is called as LC circuit. Oscillations produced by it are called LC oscillations.

Here, *ZX cXL* is the impedance and the current leads voltage by an angle 90.

Image: Phasor diagram of an LC circuit

In LC oscillations charge q, I and $\frac{d\mathcal{L}}{dt}$ all oscillate with the same angular frequency. But the phase difference is always 90. Thus we have AC: $I\Box\hspace{-1.4mm}\Box q\bigoplus\limits_{\smile}$ sin $\Box t.$ *dI dt*

AC circuit with a resistor and a capacitor:

Image: RC circuit

A circuit with a resistor and a capacitor connected in series is called a RC circuit. Here, $Z\Box \sqrt{R2\Box X2_c}$ is the impedance and the current leads voltage by an angle tan1 *^c* . *X R* \Box 叶 \Box \Box \square \Box

Image: Phasor diagram of a RC circuit

Series LCR circuit:

Impedance triangle:

Image: Impedance triangle of a LCR circuit

 \bigcirc It is a right angled triangle, whose <u>base</u> represents ohmic resistance (R), perpendicular represents reactance $\forall x$ and hypotenuse represents

impedance (Z) of the series LCR circuit as shown in figure above.

● Impedance of circuit

*Z R*2 (*LXXC*)2

Admittance:

● The reciprocal of the impedance of an ac circuit is known as admittance. It is represented by Y.

$$
\Box \text{ Admittance} = \frac{1}{\text{Impedance}} \text{ or } \angle \Box \frac{1}{Z}
$$

 \bullet The unit of admittance is ohm ^{\Box} or Siemens.

Susceptance:

● The reciprocal of the reactance of an ac circuit is known as susceptance. It is represented by S.

$$
\Box\ \text{Susceptance}=\frac{1}{\text{Reactance}}
$$

The unit of susceptance i $\wp h m$) \Box or Siemens.

```
\bigcirc Inductive susceptance =
```
1 Inductive Reactance

Or SLI
$$
\frac{1}{\chi_l} \Box \frac{1}{\Omega_l}
$$
 Capacitive susceptibilitye
$$
=
$$

1 *Capacitive* Re *ac* tan *ce*

$$
\text{Or } S_C \ \Box \frac{1}{X_C} \ \Box \frac{1}{\underline{\underline{\Pi C}}} \ \Box \Box C
$$

Resonant series LCR circuit:

● When the frequency of AC supply is such that the inductive reactance and capacitive reactance and **EX**Q**C**ual DX

● The impedance of the series LCR which is equal to the ohmic resistance in the circuit. As the current in the circuit becomes maximum. Such series LCR circuit is known as resonant series of circuit and the frequency of the

AC supply is known resonant frequenc $\mathcal{F}(f)$. The resonant frequency is

$$
\Box r \Box \frac{1}{2\Box \sqrt{LC}}
$$

$$
\Box r \Box \frac{1}{\sqrt{LC}}
$$

The series resonance circuit is known as acceptance circuit. It is used in radio and TV receiver's sets of tuning a particular radio station/TV channel.

● A circuit exhibits the resonance phenomenon if both L and C are present in the circuit. Then the voltage across L and C cancels each other. We can have resonance in an LR or RC circuit.

Image: Condition of resonance in a series LCR circuit with a graph

Parallel LCR circuit:

Image: Parallel LCR circuit

Similar to a series LCR circuit, parallel LCR circuit has:

Other quantities such as admittance, and susceptance remain the same.

Quality factor:

● It is a measure of the sharpness of the resonance. It is defined as the ratio of the reactance of either the inductance or capacitance at the resonant angular frequency to the total resistance of the circuit.

$$
Q \Box \frac{X_L}{R} \Box \frac{IIL}{R}
$$
\n
$$
Q \Box \frac{X_C}{R} \Box \frac{1}{IICR}
$$
\n
$$
\Box Q \Box \frac{1}{R} \sqrt{\frac{L}{C}}
$$

Quality factor is also expressed in terms of bandwidth *Q* Resonant frequency Bandwidth

Power in an AC circuit:

● In an ac circuit we may define three types of power.

● Instantaneous power: The power in the AC circuit at any instant of time is known as instantaneous power. it is equal to the product of values of alternating voltage and alternating current at that time.

 \bullet Average power ($P_{\rm ov}$): The power average over one full cycle of AC is known as average power. It is also known as true power.

*^V ^I PavVrmsIrms*cos00cos 2

 \bullet Apparent power: The product of virtual voltag $\mathbf{z}_{\mathsf{\scriptstyle{T}Mns}}$ and virtual current (I_{rms}) in the circuit is known as virtual power.

*^V ^I PvVrmsIrms*⁰⁰ 2

Power factor:

 \bullet It is defined as the ratio of true power to apparent power of an AC circuit

True power Apparent power $\mathsf{cos}\mathbb{I}\mathbb{I}$

● Power factor is also defined as the ratio of the resistance to the impedance of an ac circuit

 $cos \mathbb{I} \mathbb{I}$ $\frac{R}{I}$ *Z*

● It is unit-less and dimensionless.

 \bullet In pure resistive circuit,

00 ;cos 1

● In pure inductive or capacitive circuit

 \Box 2 \Box \Box ;cos \Box \Box 0

● In RL circuit,

 $Z \Box R$ R 2 $\Box X$ R and cos $\Box R$ *Z*

● In RC circuit,

 $Z \Box R$ 2 \Box X 3 nd cos $\overline{{\mathbb{H}} \mathbb{D}}^R$

● In series LCR circuit,

 $Z \Box R^2 \Box (X_L \Box X_C)^2$ and $\cos \Box \Box^R_Z$

Z

 \bigcirc At resonance, $X_L \square X_C$ *ZR* and $\Box \Box 0^0$

Watt less current:

● The average power associated over a complete cycle with a pure inductor or pure capacitor is zero, even though a current is flowing through them. This current is known as the watt less current or idle current.

Transformer:

● It is a device used for converting a low alternating voltage to a high alternating voltage and vice versa. It is based on the principle of mutual induction.

● There are two types of transformer: Step-up and Step-down transformers.

 \bullet For ideal transformer, $\frac{V_{\rm s}}{V_{\rm s}} \Box \frac{I_{\rm s}}{V_{\rm s}} \Box \frac{N_{\rm s}}{V_{\rm s}}$ *V Np*

Where k is called the transformation ratio.

 \bullet For a step-up transformer, $k > 1$. i.e. $Vs\Box Vp$, $Is\Box Ip$ and $Ns\Box Np$.

 \bullet For a step-down transformer, $k < 1$. I.e. $Vs\Box Vp$, $Is\Box Ip$ and $Ns\Box Np$.

● Power losses in a transformer are: Copper loss, Iron loss, Loss due to flux leakage, Hysteresis etc…

● Efficiency of a transformer,

Image: Types of transformers

AC generator/dynamo:

An AC generator/Dynamo produces alternating current energy from mechanical energy of rotation of a coil. It is based on the phenomenon of electromagnetic

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induction. The form of EMF induced is max.emf induced. Here, N is total number of turns in the coil, A is face of the coil, B is strength of magnetic field applied and w is angular velocity of the armature coil. $\square \square$ Dosin $\square t$, where \square ODNAB \square .

DC Generator:

A DC generator/Dynamo produces direct current from mechanical energy of rotation of a coil. Its primary and working are the same as those of AC generators. There is only a little change in the design of the generator slip ring arrangement used in AC generators is replaced by split ring arrangement in DC generators.

DC motor:

A DC motor converts direct current energy from a battery into mechanical energy of rotation. It is based on the fact that when a coil carrying current is placed in a magnetic field, it experiences a torque which may cause the coil. The efficiency back emf

8M prohibility is given by: OD

Image: DC motor

Points to remember:

Alternating current is the current which changes continuously in magnitude and in direction periodically. It can be represented by a sine curve or a cosine curve

 $I\Box I$ ^{Osin $\Box t$ </sub> Or $I\Box I$} $0 \cos t$ ● The mean or average value of alternating current voltage over one complete cycle is zero.

or or , or or 0 0 *T T Iav I I*0 0 *T* 0 sin 0 0sin *Iav Vav* 0 *dt dt V T dt dt m V V*

● Root mean square of alternating current is defined as that value of steady current, which would generate the same amount of heat in a given resistance in a given time, as is done by the alternating current when passed through the same resistance for the same time.

● The RMS value of alternating current is also known as effective value or virtual value of ac. It is represented $k_{\mathcal{M}\!\scriptscriptstyle\rm{IS}}, l_{\mathcal{\it eff}}$ or $I_{\mathcal{V}}$.

$$
I_{rms} \text{ or } M\Box \text{ } ^{1}2 \text{ } \Box 0.70710
$$

● Form factor is ratio of rms value to average value of alternating current or

$$
\begin{array}{c}\n I_o \\
\text{voltage during half cycle. Form factor} \frac{I_{rms}}{I_{\text{av}}} \square \frac{2}{2I_o} \square \frac{1}{2} \square 11.11 \\
 \square\n\end{array}
$$

● The alternating voltage is in phase with current when ac flows through a resistor but lags the voltage by a phase angle of 90 for an inductive circuit and leads the voltage by an phase angle of 90 for a capacitive **C**rituat then for an LCR circuit:

Then, *II* 0sin(*t*)

Where
$$
I_0 \square \bigvee_Z
$$

Here Z is the impedance of the series LCR circuit.

 \bigcirc The alternating current lags behind the voltage by a phase angle φ X_L $\prod X_C$ tan *R L C*

 \bullet When $X_L \,\square X_C$, tan \upphi is positive. Therefore, \upphi is positive. Hence current lags behind the voltage by a phase angle ϕ . The ac circuit is an inductance dominated circuit.

- When *X LXC* , tan ϕ is negative. Therefore, ϕ is negative. Hence current leads the voltage by a phase angle ϕ. The ac circuit is a capacitance dominated circuit.
- Impedance triangle is a right angled triangle, whose base represents ohmic resistance (R), perpendicular represents reactance (*X LXC*) and

hypotenuse represents impedance (Z) of the series LCR circuit. ● The reciprocal of the impedance of an ac circuit is known as admittance. It

is represented by Y.

 \Box Admittance = \Box 1 \Box 1 \Box *Z* or *Y* Impedance

The unit of admittance is (ohm) ¹ or Siemens.

● The reciprocal of the reactance of an ac circuit is known as susceptance. It is represented by S.

 \Box Susceptance = Reactance

The unit of susceptance l^{@hm)[]1} or Siemens.

● When the frequency of AC supply is such that the inductive reactance and capacitive reactance are equal *XLLXC*, The impedance of the series

LCR which is equal to the ohmic resistance in the circuit. As the current in the circuit becomes maximum. Such series LCR circuit is known as resonant series of circuit and the frequency of the AC supply is known resonant frequency $(\Box r)$. The resonant frequency is

$$
\begin{array}{c}\square r\square \quad \frac{1}{2\pi LC} \\ \square r\square \quad \frac{1}{LC}\end{array}
$$

● Quality factor is a measure of sharpness of resonance. It is defined as the ratio of reactance of either the inductance or capacitance at the resonant angular frequency to the total resistance of the circuit.

● Instantaneous power: The power in the AC circuit at any instant of time is known as instantaneous power. it is equal to the product of values of alternating voltage and alternating current at that time.

● Average power (*Rav*): The power average over one full cycle of AC is known as average power. It is also known as true power.

*^V ^I PavVrmsIrms*cos00cos 2

 \bullet Apparent power: The product of virtual voltag $\mathbf{z}_{\textit{rms}}$) and virtual current (I_{rms}) in the circuit is known as virtual power.

*^V*0*^I ^P^V ^I* ²⁰ *v rmsrms*

● Power factor is defined as the ratio of true power to apparent power of an AC circuit

True power $cos¹$

Apparent power

● Power factor is also defined as the ratio of the resistance to the impedance of an ac circuit

R Z $\mathsf{cos}\square$ \Box

● The average power associated over a complete cycle with a pure inductor or pure capacitor is zero, even though a current is flowing through them. This current is known as the watt less current or idle current.

● Transformer is a device used for converting a low alternating voltage to a high alternating voltage and vice versa. It is based on the phenomenon of mutual induction.

 \bullet For ide al transformer, $\frac{V}{\beta} \Box \frac{I}{\beta}$ *N* al transformer, *sk* f *V Np*

Where k is called the transformation ratio.

● An AC generator/Dynamo produces alternating current energy from mechanical energy of rotation of a coil. It is based on the phenomenon of electromagnetic induction.

● A DC generator/Dynamo produces direct current from mechanical energy of rotation of a coil. Its primary and working are the same as those of AC generators.

● A DC motor converts direct current energy from a battery into mechanical energy of rotation

Important formulas:

●The RMS value of alternating current is also known as effective value or virtual value of ac. It is represented $\bm{\mathsf{b}}_{\mathsf{M} \gamma \text{s}}$, *leff* or $\bm{\mathit{I}}_\mathsf{v}$.

I rms \bullet Similarly, for alternating voltage $\mathsf{v}_{\!r\!m\!s}$ OR *I* Then, / □/0sin(대Ⅱ) \bullet Form factor = *I* or *I v* ⁰ 0.707*I*0 2 \Box \bullet For a pure resistive circuit: Let *VV* 0sin*t V D* $\frac{V}{2}$ *D* $\frac{V}{2}$ in Dt *II* 0sin Dt *R R* ● For a pure inductive circuit: Let *VV* 0sin*t* \mathbb{H}_{H} or Then, *I* \square *I*Osin団t \square 二日 \Box 2 Where I 0 \Box $\frac{V_0}{H}$ *L* ● For a pure capacitive circuit Let *VV* 0sin*t* \Box *I***U**IOsin咀tI 只 \Box 2 Where $D\square(\square C)V0$. ● For a series LCR circuit Let *VV* 0sin*t* Where *I* $^{\prime}$ 0 $\mathbb{I}^{\mathsf{V}_{0}}$ *Z* Here Z is the impedance of the series LCR circuit. ² *^R*2*L C* ¹ *^Z ^R*² (*LX^X* ²*C*) The alternating current lags behind the voltage by a phase angle φ *X L X* tanⅢ ^{∧ L} ¤^{*r*c} \blacktriangleright Inductive reactance: $\not\!\!\!\!\mathbb{Z}$ \square \square \square \square \square \square 2 V_{rms} ^{V_0} \Box 0.70 V_0 *o* 2 $2I_o$ \Box 2 2 1.11 *rms av I I I I* \Box \sim \Box

● Average power: \bullet Apparent power P v \Box V $_{rms}$ I $_{rms}$ \Box $\frac{V_0 I}{2}$ \bigcirc Power factor: co $\mathsf{S} \square \frac{\mathsf{R}}{\mathsf{Z}}$ *C* ● Resonant frequency: $\Box r \Box \frac{1}{2\Box LC}$ $\Box r \Box$ ¹ LC \bullet Quality factor: $Q\Box$ X_L $Q\square \stackrel{X_c}{\cdot} \square \stackrel{1}{\cdot}$ *r* ● Capacitive reactance: *X* \bullet Admittance = $\left(\begin{array}{ccc} 1 & 1 \\ 1 & 1 \end{array} \right)$ or \bullet Susceptance = \bullet Inductive susceptance $_{\overline{r}_n}$ 1 *XL* \bullet Capacitive susceptance = $\frac{1}{2}$ Or SL $\begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix}$ *L* Or S $C\Box$ $\begin{matrix} 1 \\ 2 \end{matrix}$ \Box \Box \Box \Box C *XC* 1 $\Box Q \Box \frac{1}{R}$ $\frac{L}{C}$ ● Quality factor is also expressed in terms of bandwidth Resonant frequency *^Q* Bandwidth *V I* $P_{\rm av}$ □*Vrmsrms*cos**⊔ĭ**Q@os□ $1 \quad 1$ 2 *C C* 1 *Z* 1 Reactance 1 Inductive Reactance $\frac{1}{4}$ \Box \Box_{\square} \Box 1 Impedance Capacitive Reactance *Y* □ *X R DrCR* 1 *R Z rL R* 2 0 0 \Box $\overline{}$ *C* 2

Questions:

1) A small signal voltage V (t) = \mathbb{V} sin ω t is applied across an ideal capacitor

C. Then which of the following statements are true:

a) Current I (t) is in phase with voltage V (t).

- b) Current I (t) lags voltage V (t) by 180^{\degree}
- c) Current I (t) lead voltage V (t) by 90 .

d) Over a full cycle the capacitor C does not consume any energy from the voltage source.

Answer: Option c), d)

S ol uti on: When an ideal capacitor is connected with an AC voltage source, current leads voltage by 90^[]. Since, energy stored in the capacitor during charging is spent in maintaining charge on the capacitor during discharging. Hence over a full cycle the capacitor does not consume any energy from the voltage source.

2) Which of the following combinations should be selected for better tuning of an L-C-R circuit used for communication?

a) R = 20 Ω, L = 1.5 H, C = 35 μF b) R = 25 Ω, L = 2.5 H, C = 45 μF c) R = 15 Ω, L = 3.5 H, C = 30 μ F d) R = 25 Ω, L = 1.5 H, C = 45 Mf Answer: Option (c) Solution: Quality factor of an L-C-R circuit is given by, 1 *R Q L C* 1 1.5 20 3501006 1 2.5 25 45106 1 3.5 15 30106 1 $Q_1 \Box$ 1.5 500 $\frac{3}{70}$ 10.35 []40 100 15 5 90 Q_2 Q_3 Q_4 Q_5 Q_6 Q_7 Q_8 Q_9 Q_9 35 3 Q_3 \Box ¹ \Box ¹⁰⁰ ³³ 022.77 1.5 40

Clearly φ 3 is maximum of φ 1 φ 2, φ 3 and φ 4.

30

 $Q40$ 25 \Box \Box $Q40$ 25 \Box \Box $Q40$ 22.30 $\square 10^{16}$

 $45\square 10^\circ$

Hence, option (c) should be selected for better tuning of an L-C-R circuit.

List of common mistakes:

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- All of the previously stated significant issues are equally asked as numerical problems and derivations.
- It is advised to have a conceptual understanding of each topic.
- \bullet Practice the more and more numerical questions from each as well.
- \bullet Keep in mind that a rolling motion can occur both with and without slipping.

 \bullet Go over the chapter's relationships between the physical quantities again.

● Create a table or chart to show the moment of inertia for various items and forms.